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Spatial Variability of Field-Measured Soil-Water Properties¹

INTRODUCTION

Water is the medium in which biological and chemical transformations of nitrogen occur and in which nitrogen in its different forms moves and is transported in the soil profile, either to plant roots or out of the profile into drains and eventually into the groundwater. To predict nitrogen behavior in soil, therefore, one must first be able to predict water retention and movement.

Water and nitrogen movement studies are made more complex by characteristics common to most field soils: their variability and heterogeneity. These characteristics complicate analytic expressions developed to describe and predict the movement of nitrogen and water under a variety of conditions involving extensive land masses. With the development of these expressions, it is important to assess to some degree the confidence that can be attached to the predictions made by the models. It is also essential to recognize that useful predictions may be attained, even when some degree of accuracy has to be forfeited because the amount of input data is sparse and the cost of collecting data is prohibitive. Therefore, analytic expressions that require simple solutions involving a minimum of field measurements of selected soil-water variables are desirable.

The experiment had three objectives. The foremost was to evaluate the type and magnitude of spatial variation found over a field considered generally uniform relative to most cultural practices. This information is of value when assessing and evaluating the properties of an entire field on the basis of limited data from only a few locations. The second objective was to evaluate the suitability of various soil-water equations for predicting water movement under field conditions. These equations vary greatly in their assumptions and, therefore, in their complexity. Our final objective was to determine if any useful relationship could be developed between laboratory measurements of particle-size analysis, bulk density, and soil-water characteristic curves, and to study the movement of water under field conditions.

Only a few field studies have been conducted to examine the influence of spatial variation on water movement. whereas considerable effort has been made to evaluate the variation expected in soils (Beckett and Webster, 1971) and their physical characteristics (Andrew and Sterns, 1963; Jacob and Klute, 1965; Mason et al., 1957; McIntyre and Tanner, 1959; and Shaw et al., 1959), as well as their chemical characteristics (Hammond 1958). In order to evaluate the true variation in water movement that exists from place to place in any area, an unmanageably large number of

¹ Submitted for publication January 30, 1973.

samples would be required. To keep measurements within a manageable size, 20 locations within the 150 hectares were randomly selected. The same experiment was conducted on each plot, and measurements were made of particle-size distribution, bulk density, soil-water characteristic curves, water storage, water flux, hydraulic conduc-

tivity, and soil-water diffusivity at depths of 30.5, 61.0, 91.4, 121.9, 152.4, and 182.9 cm at each location. Subsequently, the measured values were used to evaluate simplified methods for determining hydraulic conductivity and flux and to estimate variability in the 150-hectare field when treated as an homogeneous unit.

FIELD SITE AND EXPERIMENTAL DESIGN

Description of experimental area

The field experiment was conducted at the West Side Field Station of the University of California, located in Fresno County 40 miles southwest of Fresno. Fresno County is in the southernmost quarter of the central valley of California, which is an elongated trough paralleling the eastern and western boundaries of the state. The valley is 500 miles long in a north-south direction and averages about 40 miles in width. The valley is surrounded by mountains except for the outlet into San Francisco Bay through which the valley rivers drain.

The climate at the West Side Field Station has two seasons of contrasting precipitation, temperature, and humidity. During the dry season (April through October) rainfall is lacking for long periods. Average temperatures are high during the cloudless midsummer days, with maximum values ranging between 38° and 43°C for a week or two at a time. The nights are generally cool and pleasant. During the rainy season (November through March) precipitation occurs as gentle rains and usually varies from 12 to 25 cm annually. The measured rainfall at the station for 1966-1971 was 10.5, 15.6, 14.9, 33.6, 17.4 and 9.3 cm per year. The growing season averages 251 days per year.

High-value crops in the area are dependent upon the availability of irrigation water. The recent development

of the California Water Plan has introduced high-quality irrigation water to the area, and the cropping pattern is changing from one of primarily barley, flax, cotton, and alfalfa to a more diversified cropping program including vegetables and tree crops. Previous to development of the California Water Plan, irrigation water was derived from either a perched water table approximately 30 feet below the ground surface and of poorquality water, or from a water table located 700 to 800 feet below the soil surface and of slightly higher water quality.

The West Side Field Station is on an alluvial fan of Panoche soil series. Panoche soils have uniform profiles but a wide range of textures. They are light brownish, grey, calcareous, friable, and permeable throughout. The source of this soil is principally the softly consolidated calcareous and gypsiferous sandstone and shale on the eastern slope of the Coast Range. They are generally free of alkali or only slightly affected.

Experimental design

In order to determine variations in rates of infiltration and redistribution in the Panoche soil, twenty 6.5-meter-square plots were randomly established over a 150-hectare site at the West Side Field Station (fig. 1). Mercury tensiometers were placed in duplicate in each plot at depths of 30.5, 61.0,

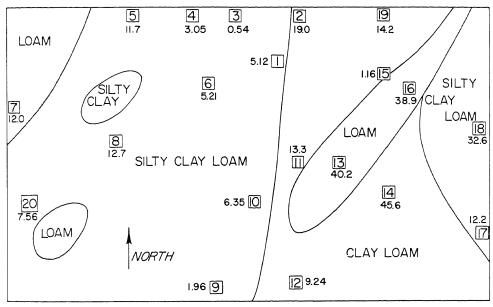


Fig. 1. Diagram of the field site showing locations of the plots (1 through 20). The number by each plot indicates the measured value of the steady-state infiltration rate (cm day⁻¹). Textures at the soil surface of the Panoche soil are also indicated.

91.4, 121.9, 152.4, and 182.9 cm to follow soil-water pressure changes during redistribution and initial wetting. Additional tensiometers were installed in five plots at 300 cm with suction probes at 300, 450, and 600 cm.

The plots were leveled and enclosed by planking installed in narrow trenches to a depth of 20 cm, and the soil was thoroughly compacted around the planking to prevent leakage. The enclosure provided 10.5 cm of free-board in which water could be ponded to any desired depth.

The tensiometers located in the center of the plot (in an area 2 meters square) consisted of a plastic barrel, a porous cup, a neoprene stopper, and a small-diameter water-filled nylon tube which connected the water in the

plastic barrel to a vertical glass tube 1 meter long, which dipped into a mercury reservoir (fig. 2). Adjacent to each glass rod was a meter stick graduated in mm to permit convenient readings of soil-water pressure. Measured values of the mercury length x (cm), together with those of distance y (cm) and soil depth z (cm), were used in the following formula to calculate the soil-water pressure head h (cm)

$$h = -(12.55 x - y - z)$$

Appendix A (see footnote for availability of appendices mentioned herein)² contains details of a Wang computer program used to calculate values of h from tensiometer readings x, y, and z.

² Positive film strips of these appendices for use in a microfilm reader are on deposit in the Agricultural Reference Service, University of California Library, Berkeley, and in the Library of The U. S. Department of Agriculture, Washington, D.C. These are identified in the card catalog as follows:

Nielsen, D. R. et al., Spatial variability of field-measured soil-water properties. Microfilm supplement, 511 pages. Hilgardia 42 (7) November, 1973.

Copies of the entire microfilm supplement may be purchased from the Library Photographic Services, University of California, Berkeley 94720. Specify LPS Misc. Microfilm No. 79.

Infiltration was initiated by ponding well water on each plot until steady-state flow was established in the profile at all depths to 182.9 cm (i.e., until mercury levels in the tensiometers remained constant). The time required for steady-state conditions was about 1 week. The rate of subsidence of the ponded water, or the rate at which water was applied to each plot, defined the steady-state infiltration rate. Chemical analysis revealed the following cations and anions present (meg per liter) in the well water: sodium, 9.6; calcium, 2.7; magnesium, 2.5; potassium, 0.1; bicarbonate, 1.4; chloride, 3.2; sulfate, 9.8; and nitrate, 0.01. The surface of the plot was covered with a 7-meter square sheet of 6-mil black plastic to prevent evaporation when infiltration was complete. The plastic was covered with a thin layer of soil to hold it in place and to prevent extreme temperature fluctuations caused by its black color. Tensiometer readings were taken hourly for the first 24 hours following infiltration and then less frequently as time passed. After 3 or 4 days following infiltration, readings were taken once a day at 8 a.m. In certain plots, tensiometer measurements were continued in excess of 100 days.

Three 7.6 by 7.6-cm soil cores were removed at each 30.48-cm depth on two opposite sides of each plot from a pit 200-cm deep dug by hand or by back hoe. Additionally, soil samples were taken from the face of each pit at 15.24-cm intervals to a depth of 182.9 cm. The samples were placed in plastic bags and taken to a glasshouse where they were dried, mixed, and sieved prior to laboratory analysis.

For obtaining core samples, soil was carefully cleared from the face of each

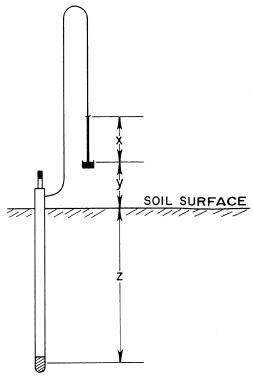


Fig. 2. Schematic diagram of tensiometer installation with porous cup at depth z, level of mercury reservoir y, and mercury length x.

pit to provide a horizontal plane into which 7.6 by 7.6-cm core cylinders could be driven and removed with an Uhland sampler. Inasmuch as three cores were taken at each 30.48-cm depth (to 182.9 cm) from each pit, a total of six cores at each depth per plot was sampled. The cores were encased in wax-coated cartons, sealed, and stored in a refrigerator prior to laboratory analysis. All leveling and depth measurements were made with a surveyor's level to that all depth measurements would be equivalent and accurate. Soil-water characteristic curves and soil-bulk density values were determined in the laboratory, using the soil cores.

LABORATORY METHODOLOGY

Particle size distribution and soil bulk density

The hydrometer method (Day, 1965) was used for determining the particle-size distribution of soil samples taken from the face of the pits on each side of every plot. These samples, which were removed at 15.24-cm intervals from 40 pits, collectively totaled 480 in number over the field.

The oven-dried weight of the soil cores obtained when the soil-water characteristic curve was experimentally determined was also used to calculate soil-bulk density. The value of the average soil-bulk density for the entire field stemmed from 720 soil cores, the sum of 120 cores at each of the six depths.

Soil-water characteristics curve

The curve describing the amount of water retained by a soil at different soil-water pressures is defined as the soil-water characteristic curve. After each of the 720 soil cores previously sealed in wax-coated cartons in the field was removed from the carton,

both ends of the core were carefully trimmed. Each core sample still containing its field soil-water content was placed in a covered glass funnel fitted with fritted-glass plates and connected to a supply of 0.01 N CaSO4 to saturate the soil. When the soil was thoroughly saturated, excess water was removed and the soil-water pressure was controlled either by a hanging water column or by air pressure. The volume of water extracted was measured and recorded for each incremental decrease in pressure. Care was taken to minimize evaporation losses. At the end of extraction, cores were dried to constant weight at 105°C. The soil-water characteristic curves for the six cores (three cores from each of two pits) taken at each depth were averaged to yield a single curve. For each plot the resulting average soil-water characteristic curve for each depth was used to relate tensiometer readings obtained in the field to soil-water content. The reliability of ascertaining soilwater content from tensiometric data in the field has been examined and discussed by LaRue et al. (1968).

FIELD METHODOLOGY AND PHYSICAL ANALYSIS

Storage

At any given time the amount of water stored at each depth was obtained from tensiometer readings. For each tensiometer reading, the water content was obtained from the soil-water characteristic curve for the particular plot and soil depth. Inasmuch as the water content from the soil surface to a depth of 30.5 cm was assumed to be identical to that at 30.5 cm, the water stored in the 0 to 30.5-cm depth was 30.5 times the water content at the 30.5-cm depth. The water stored from the soil surface to any depth L was the water stored from 0 to 30.5 cm plus that stored be-

tween 30.5 and L cm. The latter amount for any given time was obtained by fitting the water content data for 30.5, 61.0, 91.4, 121.9, 152.4, and 182.9 cm using a cubic spline function (Erh, 1972) with the aid of the computer program given in Appendix B. This function $\theta(z,t_i)$ was integrated from z equal to 30.5 to L to obtain the water stored in the profile at different times (t_i) following the cessation of infiltration. Hence, the amount of water stored S_L (cm) at time t_i was equal to

$$S_L(t_i) = 30.5 \,\theta(30.5, t_i) + \int_{30.5}^{L} \theta(z, t_i) \,dz.$$

Soil-water flux

Soil-water flux is the quantity of water leaving the profile per unit time across a specific depth. The value of the flux across depth L was calculated for each plot from the time rate of change of the amount of water stored in the profile from the soil surface to the depth L. Its value (also calculated with the computer programs given in Appendix B) is $dS_L(t)/dt$, which is the derivative of the above equation for S_L . For steady-state infiltration conditions which prevailed initially for all plots, the soil-water flux was assumed identical for all soil depths and equal to the measured steady-state infiltration rate.

Hydraulic conductivity

A measure of the rate that a particular soil will conduct water at a given water content is known as its hydraulic conductivity. It is the proportionality factor in the Darcy flow equation

$$J = -K(\theta) \nabla H \tag{1}$$

where J is the soil-water flux (cm³ cm⁻² day⁻¹), $K(\theta)$ the hydraulic conductivity (cm day⁻¹), and ∇H the hydraulic head gradient. Here, H the hydraulic head (cm) is the sum of the soil-water pressure head h(cm) and the gravitational head or vertical distance z(cm). The soil-water content is given as θ (cm³ cm⁻³).

Values of hydraulic conductivity are sensitive to small changes in water content. Characteristically, hydraulic conductivity value decreases in order of magnitude for only a small decrease in water content. It is not unusual for hydraulic conductivity values to range over a factor of 10⁵ for water contents measured in the field.

Numerous experimental methods have been developed to measure the hydraulic conductivity. These methods include steady-state columns (Klute, 1965) and field studies (Richards et al., 1956; Nielsen et al., 1961; Rose et al., 1965; LaRue et al., 1968; and Davidson et al., 1969).

Combining equation [1] with the equation of continuity

$$\frac{\partial \theta}{\partial t} = -\frac{\partial J}{\partial z}$$

gives the following basic differential equation for soil-water flow in the vertical direction

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left(K(\theta) \frac{\partial H}{\partial z} \right)$$
 [2]

where t is time in days.

In order to obtain the value of K at soil depth L, we integrate equation [2] with respect to z from the soil surface (z=0) to the desired soil depth (z=-L)

$$\int_{0}^{-L} \frac{\partial \theta}{\partial t} dz = K \frac{\partial H}{\partial z} \bigg|_{z=-L} - K \frac{\partial H}{\partial z} \bigg|_{z=0}$$
 [3]

Because there is no flow across the plastic-covered soil surface, the second term on the right-hand side of equation [3] is zero. Substituting (h+z) for H, equation [3] becomes

$$\int_{0}^{-L} \frac{\partial \theta}{\partial t} dz = K \left[\frac{\partial h}{\partial z} + 1 \right]_{z=-L}$$
 [4]

In order to use discrete experimental values in equation [4] we define $\Delta \theta = (\theta_{i+1} - \theta_i)$ and $\Delta t = (t_{i+1} - t_i)$ where the subscripts represent two different time values. For example, if $i = 1, \Delta \theta$ is the water content on day two minus the water content on day one. This designation changes equation [4] to

$$\frac{1}{t_{i+1} - t_i} \int_{o}^{-L} \left[\theta_{i+1}(z) - \theta_{i}(z) \right] dz = K(\bar{\theta}) \left(\frac{\partial \bar{h}}{\partial z} + 1 \right)$$
 [5]

where the bar above θ and h represents average values over the time period $\triangle t$. Rearranging terms in equation [5], the

value of the hydraulic conductivity is calculated from

$$K(\bar{\theta}) = \frac{1}{(t_{i+1} - t_i) \left(\frac{\partial \bar{h}}{\partial z} + 1\right)} \int_{o}^{-L} \left[\theta_{i+1}(z) - \theta_i(z)\right] dz$$
 [6]

where

$$\bar{\theta} = \frac{1}{2} \bigg[\theta_{i+1}(-L) \, + \, \theta_{i}(-L) \, \bigg]$$

and

$$\frac{\partial \tilde{h}}{\partial z} = \frac{1}{2} \left[\frac{\partial h_{i+1}}{\partial z} + \frac{\partial h_i}{\partial z} \right]$$

A smooth curve was drawn through values of h(z) using the cubic spline function in order to evaluate the slope $\partial h/\partial z$ mathematically.

Values of $K(\theta)$ were obtained from equation [6] using the program given in Appendix B.

Soil-water diffusivity

Soil-water diffusivity defined by Childs and Collis-George (1950) is somewhat difficult to visualize physically, but mathematically it is simply the product of the hydraulic conductivity at a given water content and the reciprocal of the slope of the soil-water characteristic curve at that same water

content. Hence,

$$D(\theta) = K(\theta) \frac{dh}{d\theta}$$
 [7]

Values of $D(\theta)$ are not as sensitive to changes in water content as values of the hydraulic conductivity. Maximum values are about 10^4 while minimum values are about 10^2 cm² day⁻¹ for water contents manifested in the Panoche soil.

A number of experimental techniques have been developed to measure soilwater diffusivity. These include: the outflow method (Gardner, 1956), which is based on measurement of the volume of water outflow as a function of time from a sample in a laboratory pressure cell; and an infiltration method utilizing horizontal soil columns (Bruce and Klute, 1956). In our study, diffusivity was obtained by multiplying values of $K(\theta)$ measured by the method described above times values of $dh/d\theta$ obtained from the soil-water characteristic curve. These values were introduced into equation [7], using the program given in Appendix B.

SIMPLIFIED, APPROXIMATE PHYSICAL ANALYSIS

Although analytic mathematical expressions based upon equation [2] for soil-water movement and retention are available, measurements of soil-water properties over the 150-hectare field reveal clearly that the soil is not strictly homogeneous. Because of soil variations over this (including those associated with soil depth) approximate analyses

may suffice to predict water movement within the limitations of the soil itself, and to measure soil-water properties applicable to the entire field. The following approximate methods were examined for their potential in yielding results acceptable within the limits of the soil variability. If found acceptable, they offer a relatively simple means of

characterizing soil-water properties on a field scale without the necessity of collecting huge quantities of data to be processed by costly, time-consuming analytical methods. Values derived by each approximate method were compared with those stemming from measured values of those calculated analytically.

Hydraulic conductivity: a simple field method

Inasmuch as the product of the hydraulic conductivity and the hydraulic gradient give the soil-water flux, hydraulic conductivity is usually obtained by measuring these latter two terms. For steady-state infiltration, the soilwater flux is measured at the soil surface and calculations of K are made easily. For transient conditions of a draining profile without evaporation, the rate of change in soil-water content in the profile can be used as a basis for calculating K, as was done in equation [6].

Values of $\partial \theta / \partial t$ as a function of z could be measured gravimetrically, by neutron moderation, gamma-radiation attenuation, or by any other practical means. Thus, as water content in the profile decreases owing to drainage, the value of K at different water contents can be readily calculated if $\partial h/\partial z$ is measured directly or estimated. Equation [4] may be simplified by approximating the integral with the product of the soil depth L and the rate of change of average soil-water content in the profile $\bar{\theta}$ (Black et al., 1969). Equation [4] can be further simplified by assuming that the hydraulic gradient $\partial H/\partial z$ is equal to unity, or that $\partial h/\partial z$ is zero. Hence,

$$L\frac{d\bar{\theta}}{dt} = -K \bigg|_{z=-L}$$
 [8]

Values of K calculated from equation [8] were compared with those ascertained, using equation [6].

Soil-water diffusivity: field method

Inasmuch as soil-water diffusivity is simply the product of hydraulic conductivity and the reciprocal slope of the soil-water characteristic, equation [4] can be modified to approximate the diffusivity. If equation [4] is simplified by approximating the integral with the product of the soil depth L and the rate of change of the average soil-water content in the profile $\overline{\theta}$ (with the value of the hydraulic gradient retained) it becomes

$$L \frac{\partial \bar{\theta}}{\partial t} = -K \frac{\partial H}{\partial z} \bigg|_{z=-L}$$
 [9]

Assuming that an average soil-water characteristic curve holds for the entire profile $(d\bar{\theta}/dh)(\partial h/\partial t)$ can be substituted for $\partial\bar{\theta}/\partial t$ and using the relation $D = K \ dh/d\theta$, equation [9] becomes

$$L \frac{\partial h}{\partial t} = -D \frac{\partial H}{\partial z} \bigg|_{z=-L}$$
 [10]

Hence, the value of D may be calculated for each depth L using only tensiometers. The value of $\partial h/\partial t$ is merely the time rate of change of the soil-water pressure head h obtained from tensiometer readings for depth L. The value of $\partial H/\partial z$ can be estimated using a second tensiometer above or below depth L.

Equation [10] can be further simplified by assuming that the hydraulic gradient is unity and hence,

$$L\frac{dh}{dt} = -D \bigg|_{z=-L}$$
 [11]

With equation [11], the diffusivity can be determined by using a single tensiometer at a depth L to obtain the time rate of change of the soil-water pressure head and thereby calculate D.

Values of the soil-water diffusivity

calculated from equations [10] and [11] were compared with those using equation [7]. Procedures outlined in Appendix B were used to calculate soil-water diffusivity values from each of the three equations.

Hydraulic conductivity: laboratory method

A number of investigators have explored the possibility of predicting the hydraulic conductivity of a soil from its pore-size distribution being estimated from the soil-water characteristic curve. For example, Childs and Collis-George (1950), Marshall (1958),

The equation proposed by Childs and Collis-George is

$$K = M(a^2\alpha^2 + b^2\beta^2 + c^2\gamma^2 + \ldots + 2a^2\alpha\beta + 2a^2\alpha\gamma + \ldots + 2b^2\beta\gamma + \ldots)$$
 [12]

where M is the matching factor, a, b, c, etc. are mean radii (inversely proportional to soil-water pressure) of the pore groups and α , β , γ , etc. are porosity elements. The above series termi-

nates at the largest water-filled pore size.

The equation used by Marshall, and by Millington and Quirk is:

$$K = 3600 \times 24 \frac{\gamma^2}{2\rho^2 q \eta} \frac{\theta^p}{n^2} \left(h_1^{-2} + 3h_2^{-2} + \ldots + (\alpha n - 1) h_n^{-2} \right) \dots$$
 [13]

and by Kunze et al. is

$$K = 3600 \times 24 \frac{\gamma^2}{\rho a n} \frac{\theta^p}{n^2} \left(h_1^{-2} + 3h_2^{-2} + \dots + (\alpha n - 1) h_n^{-2} \right) \dots$$
 [14]

where γ is the surface tension of water, ρ the density of water, g the acceleration due to gravity, and η the viscosity of water. For Marshall's method p equals 2 and n is the number of pore classes up to the water content of interest. In other words, n is different for calculating K at different water content. For Millington and Quirk's method, p equals 4/3 and n is the total number of pore classes. For the method of Kunze et al. p equals 1 and n is the total number of pore classes.

Soil-water characteristic curves for each depth of each plot were used to calculate values of hydraulic conductivity as a function of soil-water content. Measured and calculated values of hydraulic conductivity were matched at water-content values that prevailed during steady-state infiltration conditions. The computer program used to calculate the theoretical values of K from equations [12], [13], and [14] is given in Appendix C. The total number of pore classes used in this program were 4, 8, 16, 32, and 64.

Estimated soil-water flux

The rate of deep drainage after infiltration stops has been examined by a number of investigators (Miller and Aarstad, 1972; Robins et al., 1954; Ogata and Richards, 1957; Wilcox,

1960). Each noted that drainage occurs for many days following an irrigation. This downward movement of water through the profile has numerous implications relating to the leaching and redistribution of soluble salts and fertilizers.

Let us assume that hydraulic conductivity is an exponential function of soil-water content, such that

$$K(\theta) = K_o \exp[\alpha(\theta - \theta_o)]$$
 [15]

where K_o and θ_o are values of K and θ corresponding to steady-state infiltration conditions. The value of the constant α is chosen to provide the best fit line for known values of K and θ . Substituting equation [15] into equation [9], assuming θ to be invariant and equal to $\bar{\theta}$ to depth L, and integrating from O to t and from θ_o to θ ,

$$\theta = \theta_o - \alpha^{-1} \ln(1 + \alpha K_o t L^{-1})$$
 [16]

Differentiating equation [16] with respect to t and multiplying by the depth L yields the magnitude of the soil-water flux J_L at depth L

$$J_L = K_o(1 + \alpha K_o t L^{-1})^{-1}$$
. [17]

The ability of equation [17] to describe the soil-water flux depends upon how closely the assumption that a unit hydraulic gradient exists is met and how well equation [15] describes the values of $K(\theta)$. Values of J_L calculated from equation [17] are to be compared with values measured at each soil depth.

DETAILED ANALYSIS OF SOIL PROFILE

Most analyses of soil-water redistribution for cases involving non-homogeneous or layered soil profiles have attempted to describe the actual condition as closely as possible using soilwater properties appropriate for each soil layer (doing so would minimize the gross assumptions we have made in the previous section). Such analyses are necessarily more time-consuming, but they provide some advantages in accuracy that might not be obtained from less detailed but more rapid

methods. Comparisons of analytic and approximate methods should indicate how soil variability may determine the futility of a detailed analysis and dictate the acceptance of a simpler analysis. In the following detailed analysis, equation [2] is used to describe the redistribution of water within the 182.9 cm profile using values of $K(\theta)$ and $h(\theta)$ measured for each 30.5-cm depth.

Rewriting equation [2] by introducing $h(\theta)$ and by assuming that K is a function of time and space, we have

$$\frac{\partial \theta}{\partial h} \left| \frac{\partial h}{\partial t} \right|_{z} = \left[\frac{\partial K}{\partial z} \right|_{h} + \frac{\partial K}{\partial h} \left| \frac{\partial h}{\partial z} \right|_{t} \right] \left(\frac{\partial h}{\partial z} \right|_{t} - 1 + K \frac{\partial^{2} h}{\partial z^{2}} \right|_{t}$$
 [18]

If no water evaporates at the soil sur- profile, the following initial and face as water redistributes within the boundary conditions are applicable:

$$h = h_e(z) \qquad t = 0 \qquad z \ge 0 \tag{19}$$

$$h = h_e(z)$$
 $t = 0$ $z \ge 0$ [19]
$$\frac{\partial h}{\partial z}\Big|_{t} = 0$$
 $z = 0$ $t = 0$ [20]

$$\frac{\partial h}{\partial z}\Big|_{t} = 0 \qquad z = L \qquad t \ge 0$$
 [21]

In general, difficulty has been encountered in the theoretical analysis with respect to the boundary condition that exists at the lower boundary in unsaturated flow of water during redistribution. To bypass the difficulty, Rubin (1967) and Wang and Lakshminarayana (1968) assumed a semi-infinite medium in which the water content approaches a constant value as $z \to \infty$. Numerically, this approach is unrealistic and time-consuming.

It was noted some time ago that when water redistributes within a field

soil, the hydraulic gradient approaches unity at a given depth (Richards et al., 1956; Nielsen et al., 1964). Adopting this behavior with additional simplifications, Davidson et al. (1969) had reasonable success in prediction soil-water flux at various depths for three soils. Equation [21] assumes this behavior. Assuming

$$\Phi(z) = h(z) - h_e(z),$$

then equations [2], [3], [4], and [5] become

$$\left. \frac{\partial \theta}{\partial \Phi} \right|_{z} \left. \frac{\partial \Phi}{\partial t} \right|_{z} = \left[\left(\frac{\partial K}{\partial z} \right]_{\Phi} + \left. \frac{\partial K}{\partial \Phi} \right|_{z} \left(\frac{\partial \Phi}{\partial z} \right|_{t} + \left. \frac{2h_{e}}{\partial z} \right) \right] \left(\frac{\partial \Phi}{\partial z} \right|_{t} + \left. \frac{\partial h_{e}}{\partial z} - 1 \right) - K \left(\frac{\partial^{2} \Phi}{\partial z^{2}} \right|_{t} + \left. \frac{\partial^{2} h_{e}}{\partial z^{2}} \right) \right] (22)$$

$$\Phi = 0 \qquad t = 0 \qquad z \ge 0 \tag{23}$$

$$\frac{\partial \Phi}{\partial z}\Big|_{t} = 0 \qquad z = 0 \qquad t \ge 0$$
 [24]

$$\frac{\partial \Phi}{\partial z}\Big|_{t} = 0 \qquad z = L \qquad t \ge 0$$
 [25]

An explicit-difference scheme was set up to solve the partial differential equation [22] subject to equations [23], [24], and [25]. Equation [22] is discretized into the following equation:

$$\frac{\Phi_{i,j+1} - \Phi_{i,j}}{\Delta t} = \left\{ \left[A_{i,j} + B_{i,j} \left(\frac{\Phi_{i+1,j} - \Phi_{i,j}}{\Delta z} + C \right) \right] \left(\frac{\Phi_{i+1,j} - \Phi_{i,j}}{\Delta z} + C - 1 \right) - K_{i,j} \left(\frac{\Phi_{i+1,j} - 2\Phi_{i,j} + \Phi_{i-1,j}}{(\Delta z)^2} + D \right) \right\} E_{i,j}^{-1}$$
[26]

where

$$A_{i,j} = \frac{\partial K}{\partial z} \Big|_{\Phi_{i,j}}$$
 [27] $E_{i,j} = \frac{\partial \theta_{i,j}}{\partial \Phi_{i,j}}$ [31]

$$B_{i,j} = \frac{\partial K}{\partial \Phi_{i,j}}$$
 [28]

$$C = \frac{\partial h_e}{\partial z}$$
 [29]

$$D = \frac{\partial^2 h_e}{\partial z^2}$$
 [30]

The functional relations between K and h, θ and h, as well as the initial condition $h_e(z)$, were approximated by a spline function (Erh, 1972). The computer program for solving equation [26] is given in Appendix D.

 $\begin{array}{c} {\rm TABLE~1} \\ {\rm PARTICLE\text{-}SIZE~DISTRIBUTION~OF~PANOCHE~CLAY~LOAM~MEASURED~AT~40} \\ {\rm LOCATIONS~IN~THE~150\text{-}HECTARE~FIELD} \end{array}$

0.2.1	Sa	ind	s	ilt	Cl	ау
Soil depth -	Mean	σ	Mean	σ	Mean	σ
cm			per	cent		
0 - 15.2	25.2	10.1	26.8	6.7	48.0	3.6
15.2 - 30.5	27.5	11.6	25.5	4.9	47.0	8.6
30.5 - 45.7	26.1	11.3	26.6	6.1	47.3	8.4
45.7 - 61.0	26.4	11.9	27.4	5.9	46.2	9.5
61.0 - 76.2	29.2	10.6	28.7	8.6	42.1	7.0
76.2 - 91.4	27.6	11.3	28.8	6.6	43.6	8.7
91.4 - 106.7	24.3	12.3	31.1	6.7	44.6	9.0
06.7 - 121.9	21.1	12.5	32.8	7.5	46.1	9.5
21.9 - 137.2	21.2	13.9	32.5	7.8	46.3	10.7
37.2 - 152.4	22.1	15.4	31.9	8.9	46.0	13.8
52.4 - 177.6	21.4	15.6	35.6	10.8	43.0	11.4
.77.6 – 182.9	20.7	17.1	35.3	10.2	44.0	12.3
Over-all mean	24.4	13.5	30.2	8.3	45.2	10.5

RESULTS AND STATISTICAL ANALYSIS

Particle-size distribution

Values of per cent sand, silt, and clay for each depth of each plot are given in Appendix E. The average particle size distribution for each depth given in table 1 shows that the overall mean clay fraction of the entire field to a depth of 182.9 cm was 45.4 per cent with a standard deviation from the mean of 10.6 per cent. The percentages of sand, silt, and clay at the soil surface were 25.2, 26.8, and 48.0, respectively. Percentages of sand and clay both decrease slightly with soil depth.

The normal frequency distribution function is

$$f = \frac{1}{\sigma\sqrt{2\pi}} \exp[-(x-m)^2/2\sigma^2]$$
 [32]

where f is the frequency, m the mean, σ the standard deviation of the mean, and x the random variable. Figure 3 depicts the clay fraction histogram and the normal frequency curve for 480 samples taken from the entire field. Frequency distributions for clay and sand were considered normal, while that for silt was too irregular to be described by equation [32].

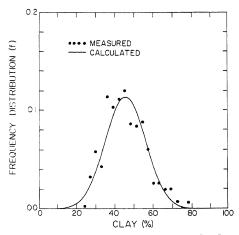


Fig. 3. Measured (480 samples) and calculated frequency distributions for clay fraction values throughout the entire field to a depth of 182.9 cm. The curve is described by equation [32] for values of m and σ equal to 45.2 and 10.5 per cent, respectively.

Soil-water characteristic

Figure 4 gives average of 120 soilwater characteristic curves for each of the six depths. Data for each soil-water pressure applied to the soil cores are given in table 2. Each curve resembles the others inasmuch as they all have the same general shape and differ only by the magnitude of the soil-water

 $\begin{array}{c} {\rm Table~2} \\ {\rm AVERAGE~SOIL\text{-}WATER~CHARACTERISTIC~VALUES~FOR~120~SOIL~CORES~FROM} \\ {\rm EACH~SOIL~DEPTH~IN~THE~150\text{-}HECTARE~FIELD} \end{array}$

	Soil-	T		Values at	different de	epths		
Characteristics*	water pressure			Soil	depth (cm)			
	head (cm)	30.5	61.0	91.4	121.9	152.4	182.9	Average
θ	-0	0.402 0.045 11.3	0.441 0.039 8.8	0.449 0.034 7.6	0.475 0.035 7.4	0.470 0.040 8.4	0.483 0.044 9.1	0.454 0.048 10.0
θ σ C.V	-10	0.396 0.042 10.6	0.433 0.035 8.2	0.440 0.031 7.0	0.465 0.033 7.1	0.465 0.038 8.2	0.476 0.042 8.9	0.446 0.048 10.8
θ σ C.V	-30	0.387 0.039 10.2	0.413 0.035 8.4	0.423 0.031 7.2	0.449 0.033 7.3	0.451 0.039 8.6	0.461 0.051 11.0	0.431 0.046 10.7
θ σ C.V	-60	0.368 0.041 11.2	0.381 0.042 11.0	0.389 0.040 10.3	0.420 0.043 10.3	0.420 0.054 12.7	0.428 0.077 18.1	0.401 0.056 13.9
θ σ C.V	-90	0.351 0.046 13.2	0.352 0.050 14.1	0.358 0.050 14.0	0.394 0.055 13.9	0.386 0.070 18.0	0.390 0.094 23.5	0.374 0.066 17.6
θ σ C.∇	-120	0.340 0.051 15.0	0.332 0.055 16.6	0.337 0.056 16.7	0.376 0.062 16.6	$0.364 \\ 0.077 \\ 21.1$	0.379 0.102 26.9	0.355 0.072 20.3
θ σ C.V	-150	0.330 0.053 15.9	0.318 0.058 18.2	0.321 0.059 18.5	0.362 0.067 18.6	0.346 0.081 23.1	0.365 0.106 29.0	0.340 0.075 22.0
<i>θ</i>	-200	0.320 0.054 17.0	0.302 0.059 19.6	0.303 0.060 19.9	0.346 0.072 20.7	0.324 0.083 25.5	0.348 0.109 31.3	0.324 0.077 23.8

* θ is the mean water content (cm³/cm³); σ is the standard deviation of the mean; and C.V. is the coefficient of variation (per cent).

content. Water contents at saturation range from 0.40 to 0.48 cm³ cm⁻³, while those at a pressure head of −200 cm range between 0.30 and 0.35 cm³ cm⁻³. Unlike hand-packed sieved samples commonly used in laboratory studies of soil water, soil cores did not manifest a capillary fringe.

Values of the standard deviation of the mean represented by the shaded areas in figure 4 increase with decreasing soil-water pressures. The standard deviations at the smaller soil-water pressures also increase with soil depth corresponding to the greater variability of the clay fraction given prevously in table 1.

If the entire field to a depth of 182.9 cm is treated as a homogeneous mass of soil, the average of 720 soil-

water characteristic curves for all six depths given in figure 5 shows that the soil-water content near water saturation can be estimated only within $\pm\,0.05~{\rm cm^3~cm^{-3}},$ while that at a pressure head of $-200~{\rm cm}$ has an uncertainty of $\pm\,0.07~{\rm cm^3~cm^{-3}}.$ Owing to the variability of the soil, and treating the soil profile as a composite of six soil layers, the soil-water content would be known no better than from $\pm\,0.03$ to $\pm\,0.11~{\rm cm^3~cm^{-3}}$ depending upon the soil-water pressure and soil depth. Soil-water characteristic data are summarized in Appendix F.

Soil-bulk density

The oven-dried weight of the soil cores revealed that soil is most compact in the top 30 cm, with bulk density

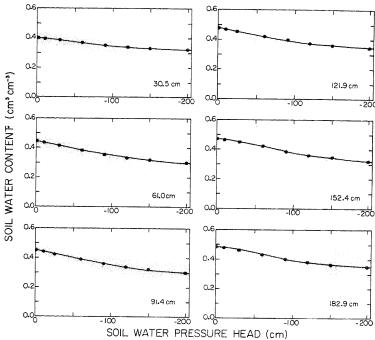


Fig. 4. Soil-water characteristic curves for the six soil depths. Each curve is the mean of the data obtained from 120 soil cores with the shaded area representing the standard deviations of the mean.

decreasing gradually with depth. The average bulk density for each 30.48-cm depth from 30.5 to 182.9 em was 1.468, 1.366, 1.348, 1.312, 1.329, and 1.313 g cm⁻³. The corresponding values of the coefficient of variation (standard deviation for the mean divided by the mean and multiplied by 100) were 10.1, 5.8, 5.8, 4.9, 4.7, and 5.9 per cent, respectively. The frequency distribution of the soil-bulk density for the entire field described by equation [32] is given in figure 6 together with measured values. The values are normally distributed. The data for each depth and plot are shown in Appendix G.

Storage

The term storage is used to describe the amount of water temporarily retained in the soil profile above a particular depth at any particular time. Figure 7 shows that the amount of water in the profile decreases monoton-

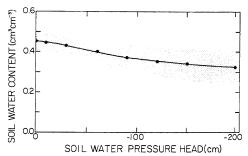


Fig. 5. Average soil-water characteristic curve for the 150-hectare field. Each point is the mean of the data from 720 soil cores, with the shaded area representing the standard deviations of the mean.

ically with time and that the amount of water stored is proportional to the depth of profile. Within the 182.9-cm profile, 76 cm of water initially stored at day zero had diminished to 61 cm following 20 days of drainage and redistribution. At the shallow depth of 30.5 cm, a total of 12 cm of water had reduced to 10 cm for equivalent times.

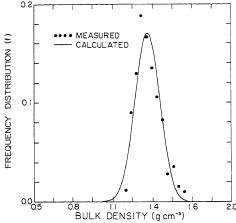


Fig. 6. Measured and calculated frequency distributions for soil-bulk density values throughout the entire field to a depth of 182.9 cm. The curve is described by equation [32] for values of m and σ equal to 1.357 and 0.0947 g cm⁻³, respectively.

The coefficient of variation was approximately 15 per cent at all depth and times. Values in figure 7 stem from measurements from all 20 plots, with the shaded areas delineating the standard deviation of the soil-water stored. Data for soil-water content and water storage for each depth and plot are given in Appendices H and I, respectively.

Soil-water flux

Corresponding to the above changes in storage, the soil-water flux increases in general with depth and decreases with time following an irrigation. For example the flux at the 121.9-cm depth for the second day following infiltration is 1.24 cm day⁻¹ and is the amount of water (cm) represented by the area be-

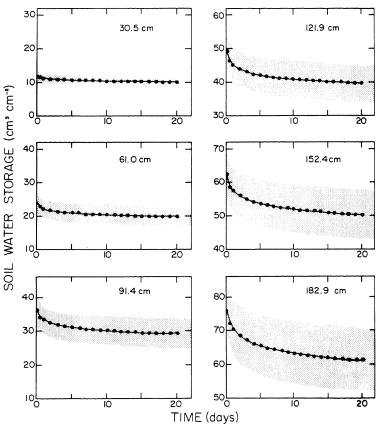


Fig. 7. Measured values of the amount of water stored (cm³ cm²) in the soil profile from the surface to different depths as a function of time after steady-state infiltration has ceased. Values given the mean values from all plots with shaded areas represent standard deviations of the means.

TABLE 3
SOIL-WATER CONTENT FOR EACH PLOT AND SOIL DEPTH DURING STEADY-STATE INFILTRATION

	T		Soil-wa	ter content	(cm ³ cm ⁻³)	at differe	nt depths*	
Plot	Infil- tration			S	oil depth (em)		
	rate	30.5	61.0	91.4	121.9	152.4	182.9	Average
	cm/day-1							
1	5.12	0.366 (99.94)	0.356 (83.24)	0.342 (78.49)	0.385 (83.54)	0.395 (86.80)	0.425 (84.95)	0.378 (86.16)
2	19.05	0.365 (100.0)	0.361 (85.38)	0.396 (92.57)	0.476 (94.33)	0.446 (85.36)	0.429 (93.97)	0.412 (91.94)
3	0.54	0.447 (99.27)	0.407 (87.18)	0.390 (81.60)	0.385 (79.38)	0.426 (85.99)	0.443 (88.88)	0.416 (87.05)
4	3.05	0.460 (95.32)	0.439 (92.58)	0.407 (84.55)	0.457 (92.94)	0.469 (93.78)	0.462 (95.59)	0.449 (92.46)
5	11.73	0.440 (100.0)	0.496 (100.0)	0.451 (100.0)	0.472 (100.0)	0.493 (100.0)	0.514 (100.0)	0.478 (100.0)
6	5.21	0.420 (93.38)	0.439 (94.45)	0.410 (88.46)	0.440 (89.38)	0.436 (93.54)	0.486 (95.52)	0.439 (92.46)
7	11.98	0.391 (98.34)	0.421 (95.94)	0.439 (99.05)	0.475 (99.46)	0.498	0.509	0.455 (98.80)
8	12.73	0.454 (100.0)	0.457 (99.85)	0.478 (100.0)	0.507 (100.0)	0.505 (98.44)	0.509 (99.43)	0.485 (99.62)
9	1.96	0.414 (99.98)	0.416 (89.42)	0.439 (93.97)	0.453 (91.58)	0.449 (97.29)	0.490 (98.11)	0.444 (95.06)
10	6.35	0.410 (97.90)	0.387 (85.40)	0.429 (92.19)	0.449 (91.67)	0.463 (95.88)	0.483	0.437 (93.12)
11	13.26	0.355 (100.0)	0.358 (99.97)	0.379 (94.80)	0.416 (96.32)	0.427 (94.95)	0.401 (91.99)	0.389 (96.34)
12	9.24	0.368 (98.66)	0.399 (89.68)	0.425 (92.84)	0.435 (91.60)	0.415 (91.99)	0.446 (94.61)	0.415 (93.23)
13	40.23	0.371 (98.96)	0.392 (97.80)	0.391 (96.47)	0.405 (97.15)	0.374 (97.42)	0.357 (91.73)	0.382 (96.59)
14	45.72	0.360 (100.0)	0.407 (100.0)	0.407	0.459	0.484	0.484	0.434 (100.0)
15	1.16	0.309 (93.55)	0.316 (71.96)	0.246 (58.91)	0.354 (84.40)	0.250 (61.29)	0.273 (65.56)	0.291 (72.61)
16	38.90	0.410 (99.47)	0.418 (99.03)	0.420 (99.38)	0.440 (98.02)	0.458	0.442 (99.42)	0.431 (98.84)
17	12.23	0.371 (99.38)	0.421 (90.11)	0.465 (96.67)	0.459 (96.28)	0.479	0.517 (100.0)	0.452
18	32.6	0.382 (100.0)	0.452 (100.0)	0. 453 (100.0)	0.447 (100.0)	0.448 (100.0)	0.512 (100.0)	0.449
19	14.20	0.420 (99.81)	0.439 (99.93)	0.488	0.485 (100.0)	0.495 (100.0)	0.497 (100.0)	0.471 (99.96)
20	7.56	0.413 (100.0)	0. 41 6 (95.85)	0.457 (98.39)	0.523 (98.42)	0.513 (99.26)	0.480 (93.34)	0.467 (97.71)
Mean	14.64	0.396 (98.70)	0.409 (92.89)	0.415 (92.41)	0.446 (94.22)	0.446 (94.00)	(93.34) 0.457 (94.49)	0.428
Standard deviation	13.38	0.0389 (2.058)	0.0411 (7.378)	0.0536 (9.923)	0.0415 (6.000)	0.0593 (8.862)	0.0607 (7.814)	(94.45) 0.0442 (6.448)

^{*} Parenthetic values are expressed as a percentage of saturation.

tween the lines marked day "1" and "2" above 121.9 cm in figure 8 divided by the time increment of 1 day. Figure 9 is a plot of the flux for the six depths aver-

aged over the 20 plots. Although the flux decreases rapidly during the first 5 days following the cessation of infiltration, water never stops moving

out of the profile during the entire experimental period. After 20 days of drainage the flux at 30.5, 61.0, 91.4, 121.9, 152.4, and 182.9 cm depths was 0.0193, 0.0398, 0.0671, 0.0973, 0.1275, and 0.1637 cm day-1, respectively.

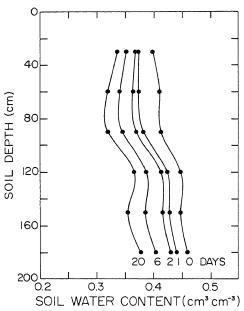


Fig 8. Soil-water-content profiles for the entire field at 0, 1, 2, 6, and 20 days following the cessation of steady-state infiltration.

After 20 days the coefficient of variation of the soil-water flux was about 30 per cent. This variability is not insignificant; in terms of the standard deviation of the 121.9 cm soil depth, it represents ± 0.3 mm per day compared with an average daily evapotranspiration loss of 6 mm. Appendix J gives the flux for each depth and each plot.

The steady-state infiltration, the average soil-water flux for the entire field, was 14.64 cm day⁻¹ with a standard deviation of the mean equal to 13.38 cm day⁻¹. The infiltration rate ranged from 0.54 cm day⁻¹ for plot 3 to 45.72 cm day⁻¹ for plot 14. Table 3 gives these values and those of soil-water content for each depth and plot. Inasmuch as the frequency distribution of the soil-water content values for all soil depths (120 values) during steady-state infiltration given in figure 10 satisfies equation [32], its distribution is considered normal.

Hydraulic conductivity

Measured values of the hydraulic conductivity determined with equation [6] are tabulated for all depths and

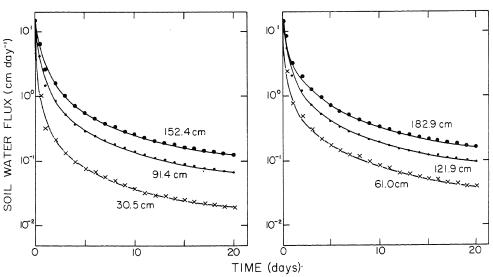


Fig. 9. Soil-water flux as a function of time after infiltration at six depths for the entire field.

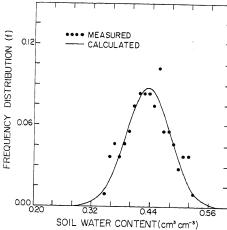


Fig. 10. Measured (120 samples) and calculated frequency distributions for soil-water contents manifested at all soil depths during steady-state infiltration. The curve is described by equation [32] for values of m and σ equal to 0.433 and 0.0455 cm³ cm⁻³, respectively.

plots in Appendix K. Values of the hydraulic gradient for each depth of each plot are given in Appendix L. A logical question to ask is: "For a specific water content what is the corresponding mean hydraulic conductivity value, and what is the value of its standard deviation?" This is a difficult question to answer. Figure 11 shows two hydraulic conductivity versus soilwater content curves at the 121.9-cm depth for plots 18 and 20. The solid square symbols in the figure represent the values during the steady infiltration. For plot 18, the steady water content was 0.448 cm³ cm⁻³ representing 100 per cent of saturation, and for plot 20 it was 0.513 cm³ cm⁻³, equivalent to 98.4 per cent of saturation. In other words, for plot 18 at a depth of 121.9 cm the water content could never exceed $0.448~\mathrm{cm^3~cm^{-3}}$ while the water content of plot 20 never fell below 0.460 cm³ cm⁻³. Under these circumstances, how can data be manipulated to obtain meaningful average hydraulic conductivity and standard deviation values with respect to a specific water content? It is physically meaningless to

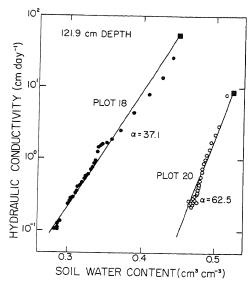


Fig. 11. Hydraulic conductivity as a function of soil-water content measured at a depth of 121.9 cm in plots 18 and 20. The solid straight lines approximating measured values stem from equation [15] for the values of α shown. The square symbol represents the steady-state value.

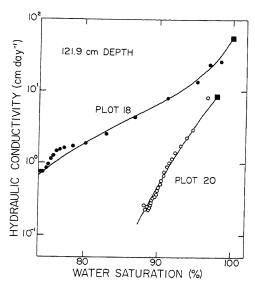


Fig. 12. Hydraulic conductivity as a function of percentage water saturation measured at a depth of 121.9 cm in plots 18 and 20. The square symbol represents the steady-state value.

extrapolate the hydraulic conductivity water content curve for plot 18 beyond its saturated water content of 0.448

*Measured data from equation [6].

HYDRAULIC CONDUCTIVITY VALUES (CM DAY-1) AT THE 30.5-CM DEPTH IN EACH PLOT FOR PERCENTAGE OF SATURATION TABLE 4

					Hy	Hydraulic conductivity values*	ıctivity value	*s:				
į						Percentage of saturation	f saturation					
rior number	100	86	96	94	86	06	88	86	84	82	80	78
1	2.55	0.485	0.0921	0.0175	0.00332	0.00063	0.00012	0.00002	< 0.00001	< 0.00001	< 0.00001	< 0.00001
2	8.89	2.13	0.513	0.123	0.0296	0.00711	0.00171	0.00041	0.00010	0.00002	< 0.00001	< 0.00001
3	0.317	0.0312	0.00308	0.00030	0.00003	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001
4	:	:	4.56	1.96	0.842	0.362	0.156	0.0670	0.0288	0.0124	0.00532	0.00229
5	70.4	4.22	0.253	0.0152	0.00091	0.00005	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001
9	:	:	:	14.4	2.74	0.524	0.100	0.0191	0.00365	0.00070	0.00013	0.00002
7	:	8.33	1.12	0.150	0.0201	0.00269	0.00036	0.00005	< 0.00001	< 0.00001	< 0.00001	< 0.00001
8	11.2	4.96	2.19	6960.	0.429	0.190	0.0838	0.0371	0.0164	0.00725	0.00320	0.00142
	0.743	0.143	0.0277	0.00536	0.00103	0.00020	0.00004	< 0.00001	< 0.00001	< 0.00001	< 0.00001	< 0.00001
10	•	2.57	1.29	0.644	0.322	0.161	0.0808	0.0404	0.0202	0.0101	0.00507	0.00254
11	11.6	4.41	1.68	0.641	0.244	0.0932	0.0355	0.0136	0.00517	0.00197	0.00075	0.00029
12	:	4.28	3.10	2.24	1.62	1.17	0.847	0.613	0.443	0.321	0.232	0.168
13	42.5	30.4	21.7	15.5	11.1	7.93	5.66	4.05	2.89	2.07	1.48	1.06
14	38.4	1.91	6.77	2.84	1.19	0.501	0.210	0.0883	0.0371	0.0156	0.00653	0.00274
15	:	:	:	0.464	0.295	0.187	0.119	0.0752	0.0477	0.0303	0.0192	0.0122
16	49.6	22.3	10.0	4.49	2.02	906.0	0.407	0.183	0.0821	0.0369	0.0166	0.00743
17	9.23	2.99	0.968	0.314	0.102	0.0329	0.0106	0.00345	0.00111	0.00036	0.00012	0.00004
18	24.4	8.86	3.21	1.16	0.422	0.153	0.0555	0.0201	0.00730	0.00265	0.00096	0.00035
19	11.2	5.86	3.07	1.61	0.843	0.442	0.231	0.121	0.0636	0.0333	0.0175	0.00914
20	3.20	0.766	0.184	0.0441	0.0106	0.00254	0.00061	0.00014	0.00003	< 0.00001	< 0.00001	< 0.00001
Mean	20.3	7.00	3.37	2.38	1.11	0.633	0.400	0.266	0.182	0.127	0.0892	0.0604
Standard deviation	21.6	8.41	5.28	4.45	2.47	1.75	1.26	0.901	0.645	0.462	0.331	0.237
						A						

20

MEAN AND STANDARD DEVIATION OF THE HYDRAULIC CONDUCTIVITY (CM DAY-1) FOR EACH DEPTH (AVERAGE OF PLOTS) AT PERCENTAGES OF WATER SATURATION FROM 100 TO 54 TABLE 5

							Hydraulic	Hydraulic conductivity	,					
Percentage of							De	Depth						
saturation	30.4	30.5 cm	61.0	61.0 cm	91.	91.4 cm	121.	121.9 cm	152	152.4 cm	182.	182.9 cm	Over-all	Over-all average
	Mean	ď	Mean	ь	Mean	ь	Mean	ь	Mean	ь	Mean	ь	Mean	ь
100	20.3	21.6	30.9	18.4	48.5	46.7	33.1	94.1	41.8	0 80				
98	7.00	8.41	18.6	13.0	27.2	6 66	93.9	17.0	0 F	40.4	48.9	37.9	35.2	30.2
96	3.37	5.28	11.7	8.46	19.6	19.4	2 20 20	19.3	1.1.2	18.9	21.4	27.3	18.6	19.8
94	2.38	4.45	7.30	5.95	12.6	13,3	11.3	0.11	1:11	6.40	13.5	17.0	12.1	13.5
92	1.11	2.47	4.48	4.39	13.2	17.8	6.97	6.15	6.54	24.0	27.7	11.4	8.05	9.42
06	0.633	1.75	3.86	3.94	8.98	11.7	4.90	4.59	4.50	0.00	9.00	7.07	6.82	11.0
88	0.400	1.26	2.30	2.25	5.99	7.67	3.27	3.47	8.98	10.0	04.7	18.5	4.87	8.10
86	0.267	0.901	2.43	3,49	4.16	5.35	2.22	2.66	2.40	3.06	7.4.0	6.01	3.37	6.11
84	0.182	0.645	1.57	2.17	2.91	3.73	1.84	2.38	1.77	9.47	7.07	9.03	2.50	4.88
82	0.127	0.462	1.01	1.42	1.99	2.72	1.25	1.72	131	00.6	0.00	0 5	1.91	3.82
80	0.0892	0.331	0.653	0.953	1.42	2.01	0.877	1.24	0.988	0.749	0.70	0.T.0	1.39	3.06
78	0.0604	0.237	0.431	0.657	1.17	1.70	0.687	1.02	1.62	1 33	i ~	707	1.00	0.40
92	0.0448	0.169	0.288	0.465	0.845	1.31	0.432	0.705	0.572	00 1	1,00	#:o:# # 2 6	0.010	2.06
74	0.0366	0.121	0.195	0.335	0.618	1.03	0.290	0.534	0.440	0000	00.0	9.04	0.012	1.70
72	0.0226	0.0864	0.155	0.257	0.457	0.816	0 203	0.419	0.440	0.00.0	1.28	3.07	0.471	1.41
70	0.0162	0.0618	0.100	0.181	0.342	0.654	0 145	0.310	0.988	00.00	1.08	2.59	0.369	1.18
89	0.0116	0.0443	0.0670	0.134	0.258	0.528	0.105	0.947	0.000	000.0	0.910	2.19	0.291	0.989
99	0.0082	0.0315	0.0461	0.102	0.196	0.427	0.0773	0 109	0.764	006.0	0.775	1.86	0.233	0.835
64	0.0058	0.0225	0.0324	0.0775	0 151	0.346	20:00	761.0	0.104	0.412	0.721	1.57	0.203	0.721
62	0.0042	0.0162	0.0931	0.0509	0.116	3 6	1100.0	0.149	0.130	0.341	609.0	1.34	0.164	0.612
60	0.0026	0 0114	0.0167	0.000	0.11.0	187.0	0.0425	0.115	0.215	0.572	0.519	1.16	0.153	0.561
58	88000	2270.0	0.0101	0.0409	0.0922	0.228	0.0318	0.0896	0.147	0.369	0.447	1.01	0.123	0.469
56	0.0016	0.0050	0.0080	0.0348	0.107	0.244	0.0238	9690.0	0.103	0.252	0.390	0.896	0.106	0.408
54.	0 0011	0.000	0.000	1040.0	0.0000	0.160	0.0180	0.0540	0.0740	0.182	0.343	0.807	0.0852	0.358
		0¥00.0	0.000	0.020.0	0.0485	0.121	0.0136	0.0420	0.0543	0.139	0.305	0.738	0.0715	0000

 ${\rm cm^3~cm^{-3}}$ to a water content of 0.513 ${\rm cm^3~cm^{-3}}$ in order to obtain an average value of hydraulic conductivity at the latter value.

We shall show later that the steady infiltration rate is highly correlated to percentage of saturation but does not correlate well with water content. Because of this correlation, it is more meaningful to express the hydraulic conductivity as a function of percentage of saturation. By this ploy, we can vary the values of hydraulic conductivity within the same domain (i.e., between 0 and 100 per cent of saturation) so that we can overcome the difficulty of evaluating the spatial variation of hydraulic conductivity due to the variation in soil-water characteristics. Figure 12 differs from figure 11 by having the hydraulic conductivity plotted against per cent water saturation. Plotting the soil-water content as percentage of saturation shifts the curves along the abscissa but the general shapes of the curves are preserved.

Table 4 lists the values of hydraulic conductivity against the percentage of saturation at the 30.5-cm depth for all plots. In table 4, any plot which has missing data beyond a certain percentage of saturation implies that for that particular plot the maximum percentage of saturation will never exceed the largest value listed. For example, for plot 4 the maximum percentage of saturation is 96 even under prolonged ponding, and for plot 6 the maximum percentage of saturation is 94. To evaluate the spatial variations of hydraulic conductivity at certain percentages of saturation, we do not intend to extrapolate beyond the maximum percentage of saturation experimentally observed. We deem this kind of extrapolation impractical because the values have no meaning even if extrapolated. Hence, in table 4 we have only 14 values of hydraulic conductivity instead of 20 at 100 per cent water saturation while at 98 per cent we have 17 values. For water-content values less than saturation, however, values of the hydraulic conductivity were extrapolated. For example, for plot 20 at the 121.9-cm depth (figure 12) measured data for water contents below 88 per cent saturation were not available. In this situation, we linearly extrapolated the semi-log plot of the hydraulic conductivity versus percentage of saturation curve to estimate values of K for water contents below 88 per cent saturation.

Table 5 lists the average hydraulic conductivity and standard deviation values at the six depths, as well as over-all average values for the field. In general, values of the standard deviation exceed those of the mean for all values of percentage of saturation. Figure 13 depicts graphs of hydraulic conductivity versus percentage of water saturation for each soil depth.

The above analysis treated the soil profile as if it were composed of six 30.48-cm layers corresponding to those depths at which measurements were made. An alternative approach can be used for calculating the mean values of the hydraulic conductivity, especially if we wish to use simplified approximate analyses where the field is treated as a homogeneous soil mass. We assume that all experimental measurements within the 150-hectare field are taken at the same time. In other words, 20 measurements are taken at each specified depth for six depths for a total of 120 experimental measurements at a time. We further assume that the measured values of soil-water content and hydraulic conductivity obtained are separate random variables which would be subject to experimental error. Table 6 illustrates how values of the average soil-water content and hydraulic conductivity can be evaluated. This table represents values of θ and K for each plot measured at 121.9 cm at times of 0, 0.5, 1, 2, 3, and 4 days. The average values of θ and K for that

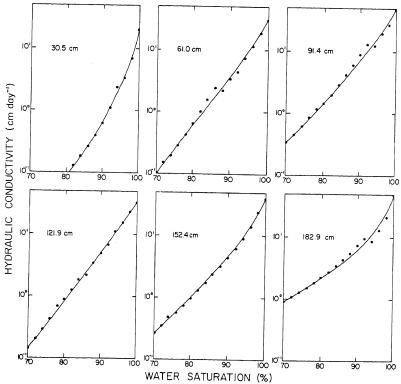


Fig. 13. Measured values of hydraulic conductivity as a function of percentage water saturation at six depths over the entire 150-hectare field. Values stem from table 5.

depth over the field for each time are given at the bottom of the table together with their standard deviation values. Such a procedure was followed for all six depths for times up to 20 days following infiltration. Figure 14 shows for each soil depth the average values of hydraulic conductivity versus average soil-water content obtained by such a procedure. These values, together with the standard deviation of the means, are tabulated for each depth and time in table 7. Although these measurements were made on the 20 plots for time periods up to 150 days, measurements were not made on plot 17 past 20 days, and hence the procedure was limited to a 20-day period.

Figure 15 depicts the over-all average hydraulic conductivity versus

average soil-water content curve for the entire field. The solid square designates the average steady hydraulic conductivity and water content. Figure 15 clearly displays an exponential relationship between hydraulic conductivity and soil-water content. For approximately every 0.045 cm³ cm⁻³ change in soil-water content the hydraulic conductivity changes an order to magnitude. The value α in equation [15] for figure 15 is 57.4. For figure 14, the values of α for each individual depth at 30.5, 61.0, 91.4, 121.9, 152.4, and 182.9 cm are 138.6, 67.5, 56.2, 52.2, 46.9, and 44.0, respectively. The values of α decreases with increasing depth.

The frequency function of a lognormal distribution is

$$f = \frac{1}{\sigma(x-\beta)\sqrt{2\pi}} \exp\{-[\ln(x-\beta) - m]^2/2\sigma^2\}$$
 [33]

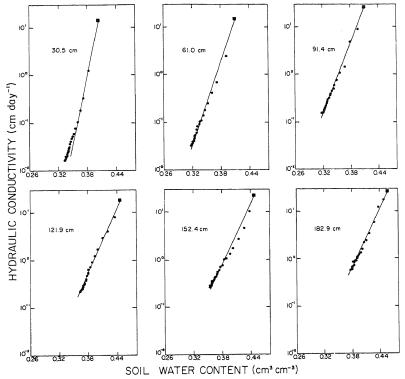


Fig. 14. Measured values of the hydraulic conductivity as a function of soil-water content at six depths over the entire 150-hectare field. Values stem from the procedure illustrated in table 6.

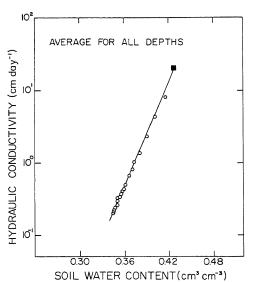


Fig. 15. Treating the entire 150-hectare field as a homogeneous soil to a depth of 182.9 cm, the graph is a plot of average hydraulic conductivity as a function of average soil-water content. The solid line is equation [15] with α equal to 57.4.

for $x > \beta$ and f = 0 for $x < \beta$, where β is any constant to allow $\ln (x - \beta)$ to be normally distributed. Figure 16 depicts the distribution of hydraulic conductivity values measured for steady-state infiltration conditions at 120 positions within the 150-heetare field and that calculated with equation [33] for values of m, σ and β equal to 2.58, 1.01, and 0 cm day-1, respectively. Apparently, values of the hydraulic conductivity for steady-state infiltration conditions are log-normally distributed.

Soil-water diffusivity

Values of the soil-water diffusivity (equation [7]) for each soil depth tabulated in table 8 are plotted as a function of percentage water saturation in figure 17. These values correspond to those of the hydraulic conductivity presented previously in fig-

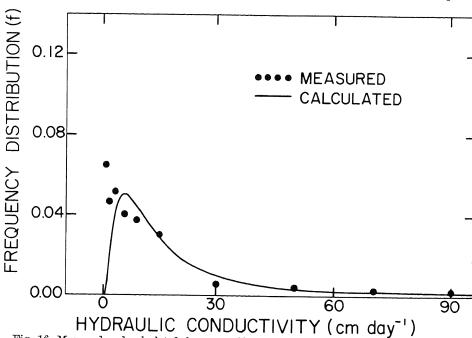


Fig. 16. Measured and calculated frequency distributions for hydraulic conductivity values for steady-state infiltration conditions. The curve is described by equation [33].

ure 13. The standard deviation of the mean soil-water diffusivity is greater than the mean. Values of D for each soil depth calculated from equation [7], using values of K given in figure 14 and the slope of soil-water characteristic curves given in figure 4, are presented in figure 18 and Appendix M. These values plotted as a function of soil-water content rather than percentage of water saturation manifest an exponential relation inasmuch as their curves are nearly linear on the semi-log graph.

Values of the soil-water diffusivity for steady state infiltration conditions measured at 120 positions satisfy equation [33]. These values like those of the hydraulic conductivity are lognormally distributed.

Hydraulic conductivity: a simple field method

A simple field method was examined by calculating the hydraulic conduc-

tivity with equation [8]. The left-hand side of the equation is an estimate of the soil-water flux at depth L at which the value of K is to be evaluated. Values of the soil-water flux according to equation ([8] are numerically equal to values of the hydraulic conductivity. An example of how well values of Kcalculated with equation [8] approximate those measured with equation [6] is given in figure 19 for all six depths of plot 1. The agreement between values is reasonable especially when the standard deviation of the mean measured values for a given water content presented previously in table 7 is considered. On the average, satisfactory agreement was obtained for all 20 plots.

Soil-water diffusivity: a simple field method

Unlike the above simple methods for estimating the hydraulic conductivity, no estimate of soil-water content or

Table 6

VALUES OF SOIL-WATER CONTENT AND HYDRAULIC CONDUCTIVITY MEASURED AT THE 121,9-CM DEPTH FOR 20 PLOTS DURING A 4-DAY PERIOD

===												
				Soil-wate	r conter	nt and hy	lraulic co	nductivi	ty values	*		
Plot	Oth	day	0.5t	h day	1s	t day	2nd	. day	3rd	day	4th	day
num- ber	θ	K	θ	K	θ	K	θ	K	θ	K	θ	K
1	0.385	6.29	0.378	5.17	0.369	4.04	0.359	1.90	0.350	1.12	0.344	0.716
2	0.476	17.7	0.464	7.98	0.445	4.25	0.430	2.06	0.419	0.956	0.412	0.610
3	0.385	0.718	0.385	0.620	0.385	0.138	0.384	0.306	0.382	0.252	0.380	0.209
4	0.457	3.83	0.452	4.69	0.446	1.21	0.437	1.99	0.426	0.962	0.421	0.752
5	0.472	14.4	0.464	1.58	0.453	5.76	0.448	12.9	0.444	7.14	0.441	5.49
6	0.440	6.46	0.439	2.78	0.436	2.42	0.429	2.30	0.422	2.07	0.416	1.65
7	0.475	13.6	0.467	7.06	0.458	1.91	0.454	1.26	0.448	0.978	0.444	0.775
8	0.507	9.87	0.495	5.51	0.480	1.87	0.474	1.06	0.468	0.711	0.463	0.510
9	0.453	1.87	0.452	2.25	0.448	1.93	0.442	1.49	0.436	1.21	0.432	0.915
10	0.449	5.83	0.444	2.50	0.437	3.02	0.427	1.97	0.416	1.14	0.409	0.728
11	0.416	17.8	0.389	9.35	0.356	1.77	0.343	0.838	0.331	0.520	0.323	0.352
12	0.435	6.80	0.429	2.85	0.417	1.81	0.404	1.07	0.394	0.688	0.387	0.494
13	0.405	42.7	0.350	14.3	0.322	3.70	0.309	3.21	0.292	1.91	0.284	1.384
14	0.459	69.2	0.423	14.5	0.377	2.43	0.355	1.18	0.336	0.686	0.326	0.418
15	0.354	39.3	0.353	0.577	0.352	0.768	0.351	0.766	0.350	0.817	0.348	0.782
16	0.440	29.2	0.426	11.0	0.408	4.45	0.397	2.56	0.387	1.48	0.380	1.01
17	0.459	18.8	0.452	10.6	0.438	8.16	0.417	4.70	0.396	2.51	0.381	1.61
18	0.447	54.7	0.440	26.2	0.426	13.6	0.408	7.91	0.388	4.40	0.371	2.49
19	0.485	32.9	0.482	26.7	0.472	14.2	0.455	7.16	0.440	2.94	0.431	2.05
20	0.523	8.74	0.514	8.13	0.503	2.95	0.449	2.24	0.494	1.78	0.491	1.43
Mean	0.446	18.3	0.435	8.06	0.421	4.02	0.411	2.94	0.401	1.72	0.394	1.22
S.D.	0.042	18.7	0.044	7.54	0.047	3.84	0.048	3.08	0.051	1.65	0.052	1.17

^{*} Values of θ and K are given in cm³ cm⁻³ and cm day⁻¹, respectively.

average amount of water stored in the profile is required to calculate the soilwater diffusivity from equations [10] or [11]. Equation [10] requires that at least two tensiometers be used to estimate the hydraulic gradient while equation [11] assumes the gradient to be unity. In both cases, a single tensiometer located at depth L suffices to estimate the value of the left-hand term of either equation. Figure 20 shows both sets of calculated values versus those measured by using equation [7] for all six depths of plot 1. For each depth the agreement is excellent if the hydraulic gradient is measured (equation [10]), and is more than satisfactory if the more simple equation [11] is used. Tabulated data for the figure and all other plots given in Appendices M, N, and O indicate that equation [11] can be used with reasonable success over the entire field.

Hydraulic conductivity from the soil-water characteristic

Agreement between values of hydraulic conductivity calculated by the equations of Childs and Collis-George and Millington and Quirk and those measured was excellent. Because values calculated by the method of Kunze et al. were nearly identical to those of Millington and Quirk using a matching factor, they are not presented. Marshall's equation was less satisfactory. Except for hydraulic conductivity values

MEAN AND STANDARD DEVIATION OF MEAN SOIL-WATER CONTENT θ AND MEAN AND STANDARD DEVIATION OF HY. DRAULIC CONDUCTIVITY K AT SIX SOIL DEPTHS FOR A 20-DAY PERIOD

Soil				Soil-wat	er content, h	ydraulic conc	Soil-water content, hydraulic conductivity, and deviation	deviation				
depth		-0	0-day*			0.	0.5-day				1-day	
	θ	ь	K	ь	θ	ь	K	ь	θ	b	100	6
cm												>
30.5	0.397	0.038	14.7	17.7	0.383	0.053	1.25	1 98	0.879	500	, 00	0
61.0	0.409	0.042	15.1	16.9	0 309	0.045	2 2	7 7	210.0	0.047	0.321	0.362
91.4	0.411	0 0 0	8 96	1 11 11 11 11 11 11 11 11 11 11 11 11 1	0.00	0.040	2.43	2.15	0.372	0.048	0.692	0.414
19.1 0	0 446	0.000	0.00	0.00	1.66.0	0.054	8.88	9.01	0.380	0.054	4.66	8.11
	0.440	0.042	18.3	18.7	0.435	0.044	8.06	7.54	0.421	0.047	4.02	3.84
197.4	0.446	0.059	22.6	23.6	0.438	0.061	10.3	9.15	0.426	0.064	4 63	4 91
182.9	0.458	0.061	26.2	30.8	0.450	0.068	17.4	21.9	0.439	0.075	12.1	18.1
average	0.429	0.054	20.6	24.7	0.416	0.058	8.11	12.1	0.402	0.062	4.40	9.10
		2.	2-day			63	3-day			4	4-day	
30.5	0.366	0.044	0.180	0.133	0.360	0.046	90 1 0	0100				
61.0	0.362	0700	0.410	0000	0000	0.040	0.102	0.073	0.356	0.046	0.0742	0.050
91.4	0960	0.00	0.410	0.230	0.353	0.050	0.248	0.128	0.347	0.051	0.179	0.085
01.1.	0.900	0.053	1.19	1.40	0.358	0.053	1.05	0.790	0.350	0.052	0.734	0.522
	0.411	0.048	2.94	3.08	0.401	0.051	1.72	1.65	0.394	0.052	1 99	10.1
152.4	0.414	990.0	3.84	2.37	0.403	0.069	1.77	1.28	0.396	0200	1.81	0.066
	0.428	080.0	5.85	7.11	0.418	0.084	3.41	3.69	0.411	0.087	2.37	2.229
average	0.392	0.063	2.35	3.79	0.382	0.064	1.38	2.11	0.374	0.066	1.04	1.56
		5-	5-day			-9	6-day			7-	7-day	
30.5	0.353	0.048	9300	0.000	0.00	0,00						
61.0	0.343	0.051	0.000	0.690	0.650	0.049	0.0515	0.0330	0.348	0.049	0.0460	0.031
91.4	0.346	0.052	0.581	0.000	0.00	0.001	0.11.0	0.0535	0.336	0.051	0.106	0.056
191 0	0380	640.0	100.0	005.0	0.044	0.052	0.486	0.407	0.340	0.052	0.441	0.377
	0000	0.000	0.920	0.098	0.385	0.054	0.715	0.461	0.382	0.054	0.648	0.577
1000	0.000	0.00	1.07	0.827	0.384	0.072	1.02	0.964	0.380	0.078	0.778	0.631
	0.*00	60.0	2.10	2.83	0.402	060.0	1.60	1.50	0.399	0.091	1.29	1.170
average	0.371	0.066	0.823	1.42	0.367	990'0	0.664	0.921	0.364	0.066	0.551	0.730
		·8	8-day			-6	9-day			10-	10-day	
30.5	0.346	0.050	0.0401	0.0306	0.345	0.050	0.0354	0.0296	0.344	0.051	0.0309	0.026
1		-			7	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			voov	0200	ח חפסה	D 048

average	0.362	0.066	0.496	0.662	0.359	0.067	0.430	0.620	0.358	0.067	0.410	0.642
		11	11-day		9	12	12-day			19	13-day	
30.5 61.0	0.342 0.328 0.331	0.051 0.052 0.053	0.0283 0.0616 0.289	0.0237 0.0368 0.282	0.341 0.326 0.329	0.051 0.052 0.053	0.0255 0.0526 0.256	0.0204 0.0287 0.258	0.340 0.325 0.328	0.052 0.052 0.053	0.0247 0.0510 0.240	0.019 0.028 0.249
121.9	0.374	0.056	0.378	0.246	0.373	0.056	0.329	0.210	0.372	0.056	0.315	0.192
152.4	0.368	0.075	0.512	0.463	0.366	0.075	0.454	0.413	0.364	0.075	0.432	0.398
182.9	0.389	0.093	1.02	1.49	0.388	0.094	0.880	0.923	0.386	0.094	806.0	1.11
average	0.355	0.068	0.374	0.568	0.354	0.068	0.334	0.512	0.352	0.068	0.329	0.568
		14	14-day			15	15-day				16-day	
30.5	0.339	0.052	0.0229	0.0175	0.338	0.052	0.0216	0.0167	0.338	0.052	0.0199	0.013
61.0	0.324	0.052	0.0454	0.0246	0.323	0.052	0.0426	0.0220	0.322	0.052	0.0405	0.022
91.4	0.326	0.053	0.220	0.228	0.324	0.053	0.202	0.211	0.323	0.053	0.189	0.198
121.9	0.370	0.057	0.289	0.173	0.369	0.057	0.275	0.168	0.368	0.057	0.263	0.162
152.4	0.362	0.075	0.391	0.344	0.360	0.075	0.366	0.332	0.359	0.075	0.352	0.328
182.9	0.384	0.091	0.824	0.968	0.383	0.095	0.703	0.742	0.381	0.095	0.840	1.06
average	0.351	890.0	0.299	0.502	0.349	0.068	0.268	0.411	0.348	890.0	0.260	0.405
		17	17-day			18	18-day			19-	19-day	
30.5	0.337	0.052	0.020	0.0154	0.336	0.052	0.0189	0.0156	0.336	0.052	0.0168	0.012
61.0	0.321	0.052	0.038	0.0221	0.320	0.052	0.0361	0.0209	0.319	0.052	0.0336	0.020
91.4	0.322	0.053	0.176	0.187	0.321	0.053	0.168	0.183	0.320	0.053	0.154	0.168
121.9	0.367	0.057	0.247	0.154	0.366	0.058	0.245	0.160	0.365	0.058	0.234	0.158
152.4	0.357	0.075	0.324	0.302	0.356	0.075	0.309	0.284	0.354	0.075	0.292	0.282
182.9	0.380	0.095	0.649	0.724	6.378	0.090	0.608	0.078	0.078	0.090	0.334	0.030
average	0.347	0.008	0.243	0.390	0.540	0.008	0.231	0.000	0.040	0.000	0.664	0.00
		30	20-day									
30.5	0.335	0.052	0.0165	0.0127								
61.0	0.318	0.052	0.0321	0.0180								
91.4	0.318	0.053	0.148	0.163								
121.9	0.364	0.058	0.229	0.170								
182.9	0.377	0.096	0.555	0.647								
average	0.344	0.068	0.209	0.344								
			1									

* Values of θ and K are given in terms of cm² and cm⁻³ and cm day⁻¹, respectively.

MEAN AND STANDARD DEVIATION OF SOIL-WATER DIFFUSIVITY (CM2/DAY-1) FOR EACH DEPTH (AVERAGE OF 20 PLOTS) AT WATER SATURATION PERCENTAGES OF 100 TO 54 TABLE 8

Water					Soil-water o	Soil-water diffusivity and deviation	l deviation					
saturation					Sζ	Soil depth (cm)						
	30.5	2	61	61.0	6	91.4	12	121.9	152	152.4	18;	182.9
	D	ь	D	Q	Q	ь	D	ь	D	ь	D	д
100	30600		45000	28300	327000	752000	136000	286000	26800	21400	487000	1280000
86	18100	27900	32300	28500	112000	246000	42800	52200	28700	35000	260000	730000
96	7490		17600	17900	42900	25900	19700	14100	16000	22600	121000	380000
94	4770		10600	11800	18500	25100	11800	8000	11000	14500	00609	206000
92	2160		8209	0608	13100	12700	7100	5490	6950	9630	37600	117000
90	1110		4416	5420	8200	8230	4950	4190	4570	6780	23800	71000
88	625		2692	3530	5280	5760	3320	3180	3090	4810	14500	42000
86	369		4425	11900	3570	4290	2260	2430	2140	3260	9460	26000
84	225	_	3453	7240	2500	3120	1870	2230	1520	2330	6040	15500
82	139	_	1713		1710	2300	1290	1640	1080	1680	4070	10000
80	87.6		892	1400	1190	1750	943	1190	785	1210	2790	0089
78	54.4		490		910	1330	730	953	573	881	1940	4200
76	34.2		284	372	099	1025	465	650	421	650	1380	2900
74	21.7	_	173		483	790	310	481	312	481	966	2100
72	13.7		131		356	610	213	364	232	362	730	1500
70	8.72		81.7		264	472	150	277	174	276	543	1200
	5.54		52.7		197	998	107	211	131	213	, 409	006
99	3.52	_	34.7		148	284	7.97	191	8.86	167	319	089
64	2.24		23.3		111	221	55.6	123	75.1	132	250	530
62	1.42		15.9		83.7	172	40.6	94.1	103	227	196	420
90	0.910	_	11.0		63.4	134	29.7	72.1	81.1	185	156	333
	0.580		7.67		93.5	227	21.9	55.3	64.3	151	124	265
	0.370		5.41	8.95	58.9	128	16.2	42.5	51.1	123	100	200
54	0.240	0.970	3.84		38.7	78.6	12.0	32.6	40.7	101	81.1	170

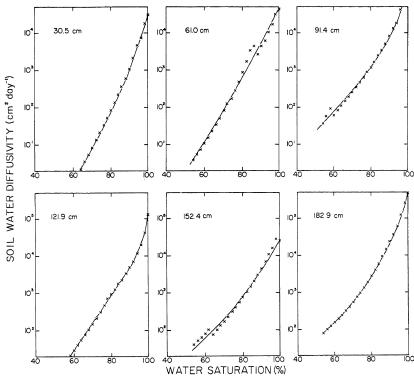


Fig. 17. Measured values of soil-water diffusivity as a function of percentage water saturation at six depths over the entire 150-hectare field. Values stem from equation [7].

calculated by the method of Kunze, et al., figure 21 shows graphs of calculated versus measured values for each of the six depths averaged over the 20 plots. Although the agreement between calculated and measured values is less satisfactory at the shallower depths, results in general indicate that the method proposed (using either of the former equations together with a steady-state infiltration matching factor) provides a satisfactory means of evaluating hydraulic conductivity properties of a field soil. By laboratory measuring the soil-water characteristic curve in the soil cores taken from the field, values of the hydraulic conductivity may be ascertained.

Estimated soil-water flux

The applicability of equations [15] and [17] to predict the soil-water flux

across a particular depth will be presented first in detail for two plots, and then for the entire field. The two straight lines in figure 11 represent the exponential approximation (equation [15]) to the measured values of K for the 121.9-cm depth of plots 18 and 20. The value of α for plot 18 is 37.1 and for plot 20 is 62.5. The straight line in figure 11 is purposely forced through the solid square symbol which denotes the values of K_o and θ_o in equation [15]. Figure 22 shows the calculated and measured soil-water flux at the 121.9-cm depth as a function of time following the cessation of infiltration for plots 18 and 20. The solid and broken lines were obtained from equation [17] with the solid and open circles being measured values. It is obvious from figure 22 that the agreement between theoretical and measured values is good for plot 18

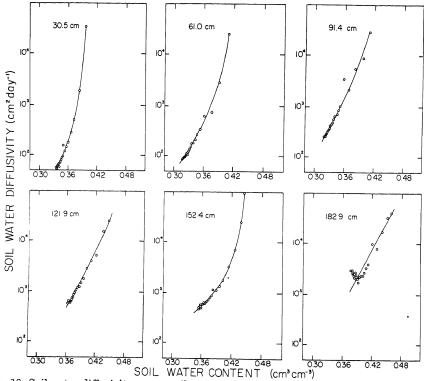


Fig. 18. Soil-water diffusivity versus soil-water content stemming from values of K in figure 14 and the slopes of the soil-water characteristic curves in figure 4.

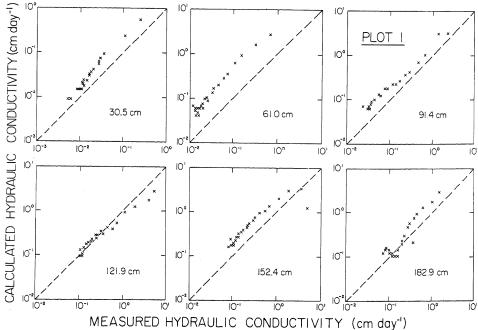


Fig. 19. Values of hydraulic conductivity calculated with the assumption that the hydraulic gradient is unity (equation [8]) versus those measured for each depth in plot 1 with equation [6].

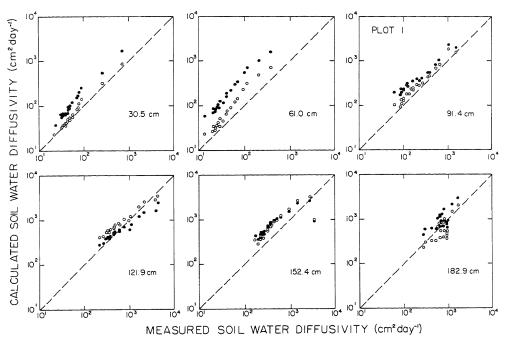


Fig. 20. Graphs of calculated values of soil-water diffusivity (open circles for equation [10] and closed circles for equation [11]) versus measured values for the six soil depths of plot 1.

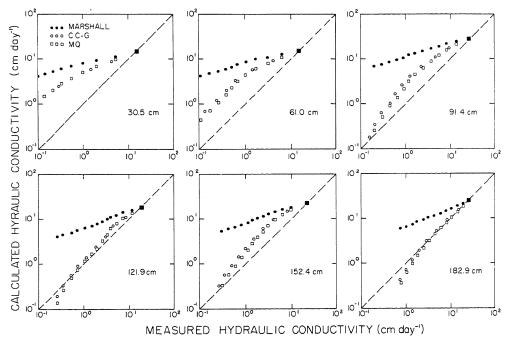


Fig. 21. Graphs of calculated values of the hydraulic conductivity versus measured values for six soil depths averaged for the entire field. Calculated values are matched with those measured for steady-state infiltration conditions.

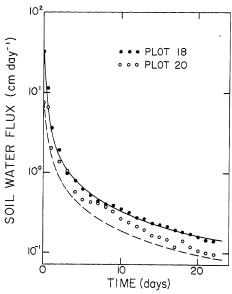


Fig. 22. Calculated (equation [17]) and measured values of soil-water flux at the 121.9cm depth for plots 18 and 20 versus time following the cessation of infiltration.

but somewhat less satisfactory for plot 20. Considering various factors which affect field measurements, plus the assumptions involved in equations [15] and [17], the agreement between theorectical and measured values is acceptable. If equation [17] is integrated with respect to time for plot 20, the total amount of drainage water calculated to leave the 121.9-cm depth during the first 22 days following infiltration was 8.85 cm, while that measured was 11.81 cm—a difference of less than 3 cm for the 22-day drainage period.

If equations [15] and [17] can be applied reasonably well to predict the soil-water behavior of individual plots, how well do they apply to the field? The values of K_o , θ_o , and α derived from the average value of K versus θ for the 150-hectare field to a depth of 182.9 cm are required. These values

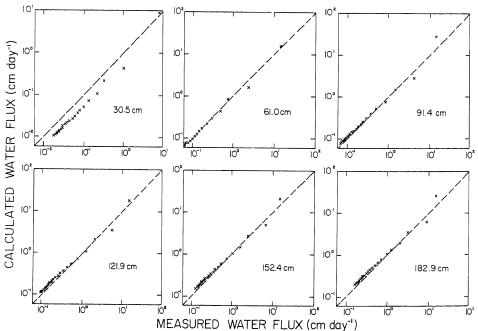


Fig. 23. Calculated (equation [17]) versus measured values of the soil-water flux for the six soil depths over the entire field for 0 to 20 days following cessation of infiltration.

given in figure 15 are 20.62 cm day⁻¹, 0.4286 cm³ cm⁻³, and 57.42, respectively. The values of α in equation [15]

is simply the slope of the curve. Figure 23 shows theoretical and measured values of the soil-water flux at the six

depths for the field. The best agreement between the calculated and experimental values is at the 121.9-cm depth. At the shallow depth, equation [17] tends to overestimate the soilwater flux and at deeper depths it underestimates it. In view of the magnitude of standard deviation presented in table 9 the theoretical values match the measured values reasonably well.

Detailed analysis of soil-water profiles

Table 10 gives the measured and calculated soil-water contents at each depth for plot 1 for the first 10 days after infiltration. Calculated values C stem from the solution of equation [26] taking into account the different

 $K(\theta)$ and $h(\theta)$ distributions for each 30.48 cm depth throughout the 182.9 cm profile. Calculated values E are those estimated with equation [16] assuming a unit hydraulic gradient and the same exponential $K(\theta)$ relation for the entire profile to depth L where the value of θ is ascertained. Although both methods of calculation yield values in close agreement with those measured, considering the effort required for the numerical analysis even without the extra complication of hysteresis sometimes included in soil-water characteristic analysis, the simplified analysis using equation [16] is entirely satisfactory, especially in view of the spatial variability of soil-water content measurements.

DISCUSSION

In an attempt to ascertain whether or not any simple relationships exist between soil physical properties measured in the laboratory or field and the movement or retention of water in the field, correlations were made statistically wherever possible.

Steady infiltration rate and steady hydraulic conductivity

Table 11 gives the correlation coefficients for steady-state infiltration rate and percentage of clay, and percentage of sand, and soil-bulk density. From the large values of the correlation coefficient it is apparent that the steady-state infiltration rate is correlated significantly to percentage of sand, percentage of clay, and bulk density at the 91.4 and 121.9-cm depths. The low values of the correlation coefficient for these properties at 30.4, 61.0, 152.4, and 182.9 cm suggest that at these depths the percentage of sand, percentage of clay, and bulk density exert no significant influence on the infiltration rate. The upper portion of the soil profile down to a depth of 60 cm is disturbed by farming operations. The soil properties at depths greater than 120 cm appear to have little influence on the redistribution of soil water. Throughout this study, it was apparent that calculations and measurements made for the 91.4 and 121.9cm depths were the most satisfactory, even though marked differences in physical properties were not manifested at these depths.

Table 12 gives correlation coefficients for steady-state hydraulic conductivity and percentage of clay, percentage of sand and soil-bulk density. As with the steady-state infiltration rate, steady-state hydraulic conductivity is correlated significantly (1 per cent level) at the 91.4 and 121.9-cm depths. The small values of the correlation coefficient for these properties at 30.4, 61.0, 152.4, and 182.9 cm suggest that at these depths and for these percentage of sands, percentages of clay and of bulk density exert no significant influence on the steady hydraulic conductivity. When all depths and plots are combined to give 120 separate measurements rather than the 20 meas-

MEAN AND STANDARD DEVIATION OF SOIL-WATER FLUX (CM DAY-1) FOR 20 PLOTS AT SIX SOIL DEPTHS FOR 0 TO 20 DAYS AFTER INFILTRATION Table 9

Time Mean σ σ Mean σ σ σ σ <						Soil-wat	Soil-water flux and deviation	eviation					
	Time					Ñ	oil Depth (cm	(1					
Mean σ </td <td>(days)</td> <td></td> <td>30.5</td> <td>9</td> <td>17.0</td> <td>6</td> <td>1.4</td> <td>12</td> <td>11.9</td> <td>15</td> <td>52.4</td> <td>31</td> <td>12.9</td>	(days)		30.5	9	17.0	6	1.4	12	11.9	15	52.4	31	12.9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		Mean	ь	Mean	ь	Mean	D	Mean	ь	Mean	ь		1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	0	14.6	13.400	14.641	13 389	14 641	10 000	11011					,
0.164 0.745 0.745 0.745 0.744 3.697 6.578 4.444 8.569 0.164 0.749 0.208 0.208 0.524 0.175 0.208 0.2045 1.020 0.341 1.196 3.199 0.011 0.496 0.208 0.110 0.524 0.175 0.752 0.245 1.020 0.341 1.196 3.199 0.075 0.221 0.075 0.274 0.111 0.531 0.152 0.719 0.213 0.907 0.083 0.174 0.054 0.240 0.0779 0.413 0.115 0.059 0.110 0.529 0.070 0.071 0.115 0.021 0.070 0.042 0.180 0.010 0.05	0.5	0.995	0.790	2.442	1 799	4 105	19.982	14.041	13.382	14.641	13.382	14.641	13.382
0.101 0.2019 0.4871 0.6892 2.088 0.964 2.621 1.196 3.199 0.111 0.4896 0.2028 0.871 0.533 1.241 0.489 1.640 0.656 2.044 0.071 0.203 0.274 0.175 0.752 0.245 1.020 0.341 1.280 0.083 0.174 0.054 0.294 0.079 0.413 0.115 0.719 0.213 0.907 0.087 0.147 0.054 0.294 0.079 0.418 0.115 0.559 0.160 0.799 0.087 0.147 0.047 0.294 0.079 0.418 0.096 0.462 0.139 0.589 0.025 0.118 0.048 0.187 0.066 0.252 0.019 0.139 0.584 0.096 0.139 0.589 0.026 0.048 0.187 0.048 0.184 0.045 0.189 0.589 0.599 0.189 0.589 0.	1	0.326	0.164	1000	1.122	4.195	2.853	5.541	3.697	6.578	4.444	8.569	2.956
0.4450 0.208 0.871 0.333 1.241 0.489 1.640 0.656 2.044 0.047 0.2480 0.120 0.524 0.175 0.752 0.245 1.020 0.341 1.280 0.045 0.221 0.054 0.1374 0.111 0.531 0.152 0.539 0.199 0.240 0.079 0.413 0.115 0.559 0.190 0.201 0.080 0.147 0.049 0.240 0.073 0.483 0.196 0.462 0.139 0.196 0.260 0.287 0.089 0.382 0.139 0.518 0.025 0.118 0.044 0.187 0.066 0.287 0.089 0.382 0.139 0.518 0.026 0.027 0.187 0.066 0.287 0.089 0.382 0.139 0.043 0.148 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075 0.075	6	010.0	# F	0.101	0.979	1.487	0.692	2.088	0.964	2.621	1.196	3.199	1.506
0.071 0.3303 0.120 0.524 0.175 0.752 0.245 1.020 0.341 1.280 0.035 0.221 0.075 0.234 0.111 0.531 0.152 0.719 0.213 0.907 0.033 0.147 0.044 0.244 0.073 0.389 0.096 0.462 0.139 0.529 0.027 0.127 0.047 0.217 0.066 0.287 0.096 0.462 0.139 0.589 0.025 0.118 0.040 0.187 0.062 0.229 0.099 0.380 0.089 0.380 0.089 0.380 0.0190 0.040 0.062 0.0190 <	c c	157.0	0.011	0.490	0.208	0.871	0.333	1.241	0.489	1.640	0.656	2.044	0 838
0.0445 0.221 0.075 0.374 0.111 0.531 0.152 0.714 0.074 0.073 0.115 0.559 0.116 0.599 0.079 0.443 0.1115 0.559 0.160 0.709 0.087 0.0147 0.0240 0.074 0.039 0.0966 0.180 0.189 0.0966 0.189 0.119 0.119 0.119 0.119 0.119 0.119 0.0196 0.0199 0.119 0.01119 0.01119 0.01119 0.011119 0.011119 0.011119 <		0.104	170.0	0.303	0.120	0.524	0.175	0.752	0.245	1.020	0.341	1.280	0.429
0.033 0.174 0.054 0.294 0.079 0.413 0.1115 0.559 0.160 0.703 0.030 0.147 0.049 0.240 0.073 0.339 0.0966 0.462 0.160 0.709 0.027 0.127 0.047 0.053 0.0966 0.462 0.139 0.589 0.025 0.118 0.048 0.187 0.066 0.252 0.075 0.139 0.512 0.020 0.096 0.048 0.187 0.066 0.055 0.097 0.037 0.018 0.054 0.051 0.075 0.139 0.512 0.020 0.084 0.048 0.149 0.0678 0.261 0.077 0.376 0.014 0.065 0.029 0.130 0.043 0.149 0.045 0.261 0.077 0.376 0.014 0.065 0.023 0.112 0.043 0.149 0.045 0.046 0.046 0.057 0.010 0.057 0.0	1 14	0.030	0.045	0.221	0.075	0.374	0.111	0.531	0.152	0.719	0.213	0 907	0.969
0.030 0.147 0.049 0.240 0.073 0.0366 0.0466 0.287 0.0966 0.462 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.582 0.139 0.043 0.043 0.044 0.048 0.048 0.048 0.049 0.054 0.075 0.099		0.077	0.033	0.174	0.054	0.294	0.079	0.413	0.1115	0.559	0.160	0 709	0.104
0.027 0.127 0.0447 0.217 0.066 0.287 0.089 0.382 0.123 0.525 0.025 0.118 0.048 0.187 0.054 0.252 0.075 0.340 0.098 0.434 0.023 0.096 0.040 0.166 0.054 0.219 0.075 0.098 0.097 0.037 0.020 0.084 0.037 0.143 0.065 0.044 0.076 0.097 0.077 0.334 0.016 0.076 0.029 0.130 0.048 0.178 0.053 0.057 0.077 0.334 0.014 0.065 0.021 0.012 0.032 0.153 0.045 0.056 0.057 0.077 0.334 0.014 0.065 0.021 0.017 0.032 0.149 0.047 0.198 0.057 0.254 0.010 0.052 0.017 0.035 0.045 0.189 0.046 0.046 0.254 0.009 0.014<		0.067	0.030	0.147	0.049	0.240	0.073	0.339	0.0966	0.462	0.139	0.589	0 167
0.025 0.118 0.048 0.187 0.062 0.252 0.075 0.340 0.098 0.431 0.023 0.096 0.040 0.166 0.054 0.219 0.0705 0.293 0.087 0.374 0.020 0.084 0.087 0.166 0.054 0.019 0.0705 0.293 0.087 0.376 0.016 0.076 0.029 0.074 0.043 0.043 0.178 0.058 0.277 0.334 0.014 0.065 0.021 0.112 0.032 0.149 0.047 0.198 0.057 0.274 0.011 0.065 0.023 0.107 0.035 0.149 0.047 0.198 0.057 0.215 0.010 0.050 0.017 0.085 0.149 0.047 0.198 0.045 0.215 0.009 0.014 0.025 0.177 0.0396 0.188 0.045 0.045 0.215 0.0094 0.047 0.014 0.0		0.057	0.027	0.127	0.047	0.217	990'0	0.287	0.089	0.382	0.123	0.512	0.144
0.023 0.096 0.040 0.166 0.054 0.219 0.0705 0.293 0.087 0.334 0.020 0.084 0.037 0.143 0.051 0.194 0.0608 0.261 0.077 0.334 0.016 0.076 0.029 0.130 0.043 0.178 0.053 0.027 0.047 0.057		0.051	0.025	0.118	0.048	0.187	0.062	0.252	0.075	0.340	860.0	0.434	0.119
0.020 0.084 0.037 0.143 0.051 0.194 0.0608 0.261 0.077 0.334 0.016 0.076 0.029 0.130 0.043 0.178 0.053 0.281 0.077 0.334 0.014 0.065 0.023 0.112 0.032 0.155 0.045 0.209 0.057 0.270 0.209 0.057 0.254 0.254 0.025 0.025 0.019 0.025 0.019 0.025 0.149 0.046 0.025 0.025 0.019 0.025 0.019 0.025 0.149 0.055 0.025 0.019 0.025 0.177 0.039 0.045 0.025 0.177 0.039 0.045 0.045 0.025 0.019 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 0.045 <		0.044	0.023	960.0	0.040	0.166	0.054	0.219	0.0705	0.293	0.087	0.376	0.106
0.016 0.076 0.029 0.130 0.043 0.178 0.0538 0.237 0.066 0.304 0.014 0.065 0.023 0.015 0.045 0.045 0.297 0.056 0.374 0.014 0.065 0.023 0.112 0.035 0.149 0.047 0.198 0.057 0.254 0.01 0.057 0.017 0.097 0.027 0.135 0.0396 0.168 0.045 0.254 0.00950 0.050 0.014 0.085 0.025 0.177 0.0379 0.168 0.045 0.254 0.00947 0.014 0.085 0.024 0.120 0.045 0.046 0.215 0.00910 0.044 0.014 0.076 0.022 0.111 0.0379 0.149 0.045 0.192 0.00910 0.044 0.013 0.070 0.022 0.111 0.0386 0.143 0.045 0.183 0.00800 0.040 0.041 0.014	TO	0.037	0.020	0.084	0.037	0.143	0.051	0.194	0.0608	0.261	0.077	0.834	0.100
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	11	0.034	0.016	0.076	0.029	0.130	0.043	0.178	0.0538	0.237	0.066	0.304	0.09
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1.6	0.030	0.014	0.065	0.021	0.112	0.032	0.155	0.045	0.209	0.057	0.520	0.0.0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	T9	0.029	0.014	0.062	0.023	0.107	0.035	0.149	0.047	0.198	0.055	0.254	0.000
0.010 0.052 0.015 0.090 0.025 0.177 0.0379 0.168 0.045 0.215 0.00950 0.050 0.014 0.024 0.024 0.120 0.0378 0.162 0.045 0.215 0.00947 0.047 0.014 0.070 0.022 0.111 0.0389 0.149 0.045 0.192 0.01000 0.044 0.013 0.076 0.022 0.108 0.036 0.143 0.045 0.183 0.01000 0.041 0.014 0.070 0.023 0.108 0.036 0.134 0.045 0.173 0.00860 0.040 0.013 0.067 0.021 0.021 0.035 0.134 0.045 0.173	14	0.027	0.011	0.057	0.017	0.097	0.027	0.135	0.0396	0.180	0.046	0.931	0.002
0.00950 0.056 0.014 0.085 0.024 0.120 0.0378 0.162 0.046 0.2010 0.00947 0.044 0.014 0.079 0.022 0.111 0.0339 0.149 0.046 0.206 0.00910 0.044 0.013 0.076 0.022 0.118 0.036 0.143 0.045 0.192 0.01000 0.041 0.014 0.076 0.022 0.108 0.036 0.143 0.045 0.183 0.00860 0.040 0.014 0.070 0.021 0.097 0.021 0.045 0.173 0.00860 0.040 0.013 0.067 0.021 0.027 0.025 0.173 0.045 0.173	cT	0.025	0.010	0.052	0.015	0.090	0.025	0.177	0.0379	0.168	0.045	0.201	0.00
0.00947 0.047 0.014 0.079 0.022 0.111 0.0389 0.149 0.043 0.192 0.00910 0.044 0.013 0.076 0.022 0.118 0.036 0.143 0.045 0.192 0.01000 0.041 0.014 0.070 0.023 0.100 0.0356 0.134 0.045 0.183 0.00860 0.040 0.013 0.067 0.021 0.025 0.134 0.045 0.173 0.0257 0.0257 0.128 0.045 0.0173 0.021 0.0257 0.128 0.045 0.173		0.024	0.00950	0.050	0.014	0.085	0.024	0.120	0.0378	0.162	0.046	0.515	0.049
	17	0.022	0.00947	0.047	0.014	0.079	0.022	0.111	0.0339	0 149	0.043	007.0	0.040
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	T8	0.021	0.00910	0.044	0.013	0.076	0.022	0.108	0.036	0.143	0.045	0.192	0.046
0.00860 0.040 0.013 0.067 0.021 0.097 0.0257 0.128 0.040	19	0.020	0.01000	0.041	0.014	0.070	0.023	0.100	0.0356	0.134	0.045	0.100	0.049
	70	0.019	0.00860	0.040	0.013	0.067	0.021	0.097	0.0257	0.128	0.044	0.164	0.049

MEASURED AND CALCULATED SOIL-WATER-CONTENT DISTRIBUTIONS FOR 0 TO 10 DAYS AFTER INFILTRATION (PLOT 1) Table 10

									Soil depth (cm)*	h (cm)*								
Days		30.5			61.0			91.4			121.9			152.4			182.9	
	w*	*5	*	×	Ö	闰	¥	Ö	闰	M	O	Ħ	M	C	Ð	M	C	囝
0	0.366	0.366	0.366	0.356	0.356	0.356	0.342	0.342	0.342	0.385	0.385	0.385	0.395	0.395	0.395	0.425	0.425	0.425
0.5	0.355	0.337	0.356	0.331	0.292	0.343	0.324	0.304	0.326	0.372	0.369	0.368	0.390	0.358	0.382	0.425	0.403	0.419
1	0.353	0.332	0.353	0.317	0.278	0.336	0.307	0.291	0.318	0.365	0.358	0.360	0.380	0.348	0.373	0.425	0.400	0.414
2	0.350	0.328	0.350	0.301	0.266	0.326	0.295	0.280	0.308	0.354	0.350	0.349	0.459	0.339	0.361	0.409	0.398	0.407
3	0.347	0.325	0.348	0.291	0.260	0.319	0.287	0.276	0.301	0.346	0.346	0.343	0.346	0.334	0.353	0.399	0.396	0.402
4	0.345	0.323	0.347	0.285	0.256	0.314	0.283	0.272	0.296	0.342	0.344	0.338	0.336	0.331	0.347	0.392	0.396	0.398
5	0.343	0.322	0.346	0.280	0.254	0.310	0.278	0.270	0.292	0.338	0.342	0.334	0.329	0.329	0.341	0.387	0.395	0.394
6	0.342	0.321	0.345	0.277	0.252	0.307	0.276	0.269	0.289	0.335	0.341	0.331	0.323	0.327	0.337	0.382	0.395	0.392
7	0.341	0.320	0.345	0.274	0.250	0.304	0.273	0.268	0.286	0.332	0.339	0.328	0.318	0.325	0.333	0.379	0.394	0.389
8	0.339	0.320	0.344	0.272	0.249	0.302	0.271	0.267	0.284	0.330	0.338	0.326	0.313	0.324	0.330	0.376	0.394	0.387
9	0.339	0.319	0.344	0.270	0.248	0.300	0.269	0.266	0.281	0.327	0.337	0.324	0.310	0.322	0.327	0.375	0.393	0.385
10	0.338	0.319	0.343	0.268	0.248	0.298	0.267	0.265	0.279	0.325	0.336	0.322	0.306	0.320	0.324	0.373	0.393	0.383
* M Measured values; C Calcul	d values;	; C Cal	culated v	ated values from equation [26]; E Calculated values from equation [16]	m equati	on [26];	E Cal	culated v	ralues fro	om equat	ion [16]							

TABLE 11
CORRELATION COEFFICIENTS BETWEEN STEADY INFILTRATION RATE AND PERCENTAGE OF CLAY, PERCENTAGE OF SAND, AND BULK DENSITY

Soil		Correlation	n coefficient	
depth	Clay	Sand	Bulk density	Sample size
cm				
30.5	-0.447	0.468	0.125	20
61.0	-0.416	0.408	0.272	20
91.4	-0.501	0.470	0.518	20
21.9	-0.524	0.492	0.615	20
152.4	-0.366	0.233	0.263	20
.82.9	-0.367	0.172	0.379	20

Table 12 CORRELATION COEFFICIENT BETWEEN STEADY-STATE HYDRAULIC CONDUCTIVITY K_o AND PERCENTAGE OF CLAY, PERCENTAGE OF SAND, AND BULK DENSITY

Soil depth	Correlation coefficient					
	Clay	Sand	Bulk density	Sample size		
cm						
30.5	-0.116	0.190	-0.121	20		
61.0	-0.230	0.287	0.213	20		
91.4	-0.519	0.546	0.474	20		
121.9	-0.681	0.644	0.571	20		
152.4	-0.430	0.336	0.180	20		
182.9 entire	-0.389	0.118	0.403	20		
field	-0.389	0.238	0.129	120		

urements available for each depth, correlation between steady hydraulic conductivity and the clay fraction is significant at the 1 per cent level and the correlation coefficient for the sand fraction represents 5 per cent significance. Correlation between bulk density and steady-state hydraulic conductivity is not significant on the combined samples. The silt fraction does not correlate significantly with either steady-state infiltration or steady-state hydraulic conductivity.

Table 13 gives correlation coefficients between steady-state infiltration rate and steady water content, as well as the correlation coefficients between steady-state infiltration rate and

steady-state per cent saturation. There are two separate sets of correlation coefficients in table 13—one to test the linear relationship between the variables, and the other to test the degree of logarithmic dependence of the variables. The small values for the correlation coefficients indicate that the steady-state infiltration rate is not linearly related to the steady-state soilwater content. The data in table 13 indicate that there is some tendency toward an exponential dependence of the steady-state infiltration rate and the steady-state water content at the 91.4 and 121.9 cm depths, although the correlation is not sufficiently high to be significant. In contrast to the linear

comparison, the logarithmic relation in table 13 indicates a strong exponential dependence between the infiltration rate and percentage of saturation. For a sample size of 20, based on significant levels of 5 per cent, 2 per cent, 1 per cent, the correlation coefficients need to be equal to 0.444, 0.515, 0.561, and 0.679, respectively. The relationship between the logarithm of the steady-

state infiltration rate and the steadystate per cent saturation at the 121.9-cm depth is significant at the 1 per cent level, indicating that there is almost a complete correspondence between these two values. The data in table 13 demonstrate that for field measurements the use of percentage of saturation is superior to soil-water content when describing soil-water movement. The per-

TABLE 13

CORRELATION COEFFICIENT BETWEEN STEADY-STATE WATER CONTENT θ_o AND LINEAR AND LOGARITHMIC STEADY INFILTRATION RATE I_o AND
BETWEEN STEADY-STATE PERCENTAGE OF SATURATION S_o AND
LINEAR AND LOGARITHMIC STEADY-STATE INFILTRATION RATE

Soil depth	Correlation coefficient				
	$ heta_o ext{ vs } I_o$	θο vs ln Io	So vs Io	So vs ln Io	Sample size
cm					
30.5	-0.2431	-0.1887	0.3738	0.4467	20
61.0	0.1099	0.2357	0.5508	0.6664	20
91.4	0.1553	0.4067	0.5184	0.7243	20
121.9	0.0997	0.4094	0.5864	0.8134	20
152.9	0.1282	0.3723	0.3855	0.5567	20
182.9	0.0153	0.2479	0.3570	0.5548	20

centage of saturation may well serve as an indicator of the effective area through which water is conducted. Usually, hydraulic conductivity measurements are made as a function of soilwater content on a volume basis without any knowledge of the percentage of saturation. This study shows that both are important, especially when the soil properties vary spatially.

Although the reasons are not readily apparent, examination of tables 11, 12, and 13 reveals that the flow characteristics of this 150-hectare field are most closely correlated with properties of the soil between 91.4 and 121.9 cm. The present field was cut, filled, and graded before farming began. Although no distinctive, well-defined horizon has been observed in the soil profile, this study clearly shows that the 91.4 to 121.9-cm depth is important in determining how water flows

through the soil profile. Thus, it is supposed that for a naturally developed field soil there may be a particular horizon whose physical properties should dictate the soil-water transport characteristics. Accumulation of knowledge on what is the most appropriate layer to use for simplified approaches on various types of soil would be most helpful in predicting soil-water behavior.

Hydraulic conductivity

We have discussed two alternatives for evaluating the spatial variation of hydraulic conductivity. First, by representing the hydraulic conductivity as a function of percentage of saturation, we were able to estimate the variation of hydraulic conductivity with respect to any specific percentage of saturation. It is obvious from table 5 that gen-

erally the coefficient of variation of hydraulic conductivity increases with decreasing percentage of saturation. The spatial variation of the soil-physical properties at the 30.5-cm depth is largest among the six different depths. This reflects the spatial variation of the hydraulic conductivity at the 30.5cm depth. The coefficient of variation ranges from about 100 per cent at saturation to about 400 per cent at 54 per cent of saturation. Coefficients of variation of hydraulic conductivity for the other five depths range from less than 100 to about 300 per cent. For the over-all average, which includes horizontal as well as vertical variation, coefficients of variation ranges from 85 per cent at saturation to 450 per cent at 54 per cent saturation.

In the second method we regard the field as a homogeneous soil mass, and we treat soil-water content and hydraulic conductivity as two separate experimental variables which would be measured from time to time. Thus, at each individual depth we will have 20 replications in terms of soil-water content and hydraulic conductivity. For the six depths, we would obtain 120 values of water content and hydraulic conductivity at any particular time period. Using this approach of averaging the soil-water content and the hydraulic conductivity at incremental time periods, the data in table 7 and figure 14 were obtained. These data represent the mean hydraulic conductivity-water content relationship for the entire field.

$$F(x', y') = \frac{1}{2\pi} \iint \exp[-(x'^2 + y'^2)/2] dx' dy'$$
 [34]

Next we introduce two new variables x and y which are correlated and are normally distributed. We relate x, y, and x', y' by the following equations

$$x = m_1 + \sigma_1 x' \qquad [35]$$

$$y = m_2 + r\sigma_2 x' + \sqrt{1 - r^2} \sigma_2 y'$$
 [36]

Equations [35] and [36] are so arranged that the new variables x and

Soil-water flux

In the application of equation [17], it is clear that both the steady-state hydraulic conductivity K_o and the slope α of equation [15] play important roles. Suppose we know the values of the steady-state water content θ_0 and K_o , and that we have knowledge of the soil-water characteristic. Then, using the method of Childs and Collis-George or that of Millington and Quirk. we can calculate the relation of $K(\theta)$. and thus evaluate the value of α at (K_o, θ_o) .

Considering the spatial variability of the entire field, the question arises: For an average value of the soil-water content and its standard deviation. what is the corresponding mean value of the hydraulic conductivity and its standard deviation? We have worked out the answer for only the steadystate values of the hydraulic conductivity and soil-water content. We found that the steady-state water content θ_o was normally distributed (equation [32]) and that the value of K_o was log-normally distributed (equation [33]). The correlation coefficient of θ_o and $\ln K_o$ was 0.327, which is significant at the 1 per cent level for 120 samples.

In order to determine for any particular θ (in the case of steady state, $\theta = \theta_o$) what is the corresponding value of K (in the steady state case, $K = K_o$) and its variation, let us consider two independent variables x' and y', each of which is normal (0, 1), their joint distribution function is

$$-(x^2+y^2)/2j ax ay$$
 [54]

y have the means m_1 and m_2 , the standard deviations σ_1 and σ_2 , and the correlation coefficient r. Rearranging equations [35] and [36], we obtain

$$x' = (x - m_1) \sigma_1^{-1}$$
 [37]

$$y' = \frac{1}{\sqrt{1 - r^2}} \left[-r \left(\frac{x - m_1}{\sigma_1} \right) + \frac{y - m_2}{\sigma_2} \right]$$

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Equation [34] as a function of the new variables becomes

$$F(x, y) = \frac{1}{2\pi} \int \int D \exp[-Q(x, y)/2] \, dx \, dy$$
 [39]

where

$$Q(x,y) = \frac{1}{1-r^2} \left[\frac{(x-m_1)^2}{\sigma_1^2} - \frac{2r(x-\xi_1)(y-m_2)}{\sigma_1\sigma_2} + \frac{(y-m_2)^2}{\sigma_2^2} \right]$$

and D is the Jacobian

$$D = \begin{vmatrix} \frac{\partial x'}{\partial x} & \frac{\partial x'}{\partial y} \\ \frac{\partial y'}{\partial x} & \frac{\partial y'}{\partial y} \end{vmatrix}$$

The joint frequency function of x and y according to (Cramer, 1955) is

$$f(x, y) = \frac{1}{2\pi \sigma_1 \sigma_2 \sqrt{1 - r^2}} \exp[-Q(x, y)/2]$$
 [40]

Equation [40] is the general form of the two-dimensional normal frequency function. If we denote $x = \ln z$, then equation [40] becomes

$$f(z, y) = \frac{1}{2\pi \sigma_1 \sigma_2 z \sqrt{1 - r^2}} \exp[-Q(x, y)/2]$$
 [41]

where

$$Q(z, y) = \frac{1}{1 - r^2} \left[\frac{(\ln z - m_1)^2}{\sigma_1^2} - \frac{2r(\ln z - m_1)(y - m_2)}{\sigma_1 \sigma_2} + \frac{(y - m_2)^2}{\sigma_2^2} \right]$$

As shown earlier, the steady-state hydraulic conductivity K_o is log-normally distributed. Rewriting equation [33] in terms of K_o and choosing $\beta = 0$, we have

$$f_1(K_o) = \frac{1}{\sigma_1 K_o \sqrt{2\pi}} \exp\left[\frac{-(\ln K_o - m_1)^2}{2\sigma_1^2}\right]$$
 [42]

Similarly, because the steady-state water content θ_0 is normally distributed we rewrite equation [32] in terms of θ_0

$$f_2(\theta_o) = \frac{1}{\sigma_0 \sqrt{2\pi}} \exp\left[\frac{-(\theta_o - m_2)^2}{2\sigma_2^2}\right]$$
 [43]

Their joint distribution function according to equation [41] is

$$f(K_o, \theta_o) = \frac{1}{2\pi \sigma_1 \sigma_2 K_o \sqrt{1 - r^2}} \exp[-Q(K_o, \theta_o)/2]$$
 [44]

where

$$Q(K_o, \theta_o) = \frac{1}{1-r^2} \left[\frac{(\ln K_o - m_1)^2}{\sigma_1^2} - \frac{2r(\ln K_o - m_1)(\theta_o - m_2)}{\sigma_1\sigma_2} - \frac{(\theta_o - m_2)^2}{\sigma_2^2} \right]$$

Then the conditional frequency function of the steady-state hydraulic conductivity relative to any other value of another steady state water content θ'_o is the following:

$$\frac{f(K_o, \theta_o')}{f_2(\theta_o')} = \frac{1}{\sqrt{2\pi} \sigma_1 K_o \sqrt{1 - r_2}} \exp \left[\frac{-\left[\ln K_o - m_1 - \frac{r\sigma_1}{\dot{\sigma}_2} (\theta_o' - m_2)^2\right]}{2\sigma_{1o}(1 - r_o)} \right]$$
[45]

Equation [45] is a normal frequency function in K_o (steady-state hydraulic conductivity) with the mean value

$$m_3 = m_1 + r\sigma_1(\theta'_o - m_2) \ \sigma_2^{-1}$$
 [46]

and standard deviation

$$\sigma_3 = \sigma_1 \sqrt{1 - r^2} \tag{47}$$

If we denote ϵ as the arithmetic mean of K_o and τ its corresponding standard deviation, then the following relations are established (Johnson and Leone, 1964):

$$\epsilon = \exp[m_3 + \sigma_3^2/2] \tag{48}$$

$$\tau = \exp[m_3 + \sigma_3^2/2] \sqrt{\exp(\sigma_3^2 - 1)}$$
 [49]

Applying equations [45], [46], [47], [48], and [49] we are able to estimate the mean and standard deviation of the steady-state hydraulic conductivity relative to any given soil-water content based on the distributions depicted in figures 10 and 16. Table 14 gives a comparison between calculated and measured values of the mean and standard deviation of K_o for the six different depths.

The statistical approach briefly given above should be an appropriate method in any kind of field study. From table 14, we know that at a depth of 182.9 cm the average value of θ_0 is 0.458 cm³ cm⁻³ corresponds to a

Table 14 MEAN STEADY-STATE WATER CONTENT θ'_o VERSUS MEASURED AND CALCULATED (EQUATIONS [48] AND [49]) MEAN STEADY-STATE HYDRAULIC CONDUCTIVITY ϵ AND ITS STANDARD DEVIATION OF THE MEAN τ

Soil depth	θο	€(cm day-1)		au (cm day-1)	
		Measured	Calculated	Measured	Calculated
cm	cm3 cm-3				
30.5	0.397	14.74	17.12	17.69	20.41
61.0	0.409	15.05	18.40	16.22	21.92
91.4	0.411	26.83	18.53	35.52	22.08
21.9	0.446	18.27	22.66	18.65	27.00
52.4	0.446	22.64	22.67	23.59	27.01
82.9	0.458	26.16	24.24	30.75	28.88
verage	0.429	20.62	20.53	24.73	24.46

calculated average value of K_o equal to 26.2 cm day⁻¹. Utilizing this pair of values as a matching factor for the Millington and Quirk method, theoretical values of K verses θ are available. Figure 24 shows the calculated

and measured values of $K(\theta)$ at the 182.9-cm depth. The open circles designate the experimental data and the solid line represents the calculated values. The square symbol designates the matching point $(K_{\theta}, \theta_{\theta})$. The value

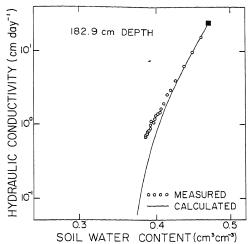


Fig. 24. Data points are measured values of the hydraulic conductivity as a function of sommater content for the 182.9-cm depth averaged over the entire field. The solid line depicts values calculated by the Millington and Quirk method using the matching factor (K_o,θ_o) equal to (26.2 cm day¹, 0.458 cm² cm⁻²). Circles designate experimental values. Square indicates matching point.

of α for the measured function $K(\theta)$ at the 182.9-cm depth is 44.0. The slope of the solid line at the point represented by the solid square is 43.2 which we regard as an approximation of α . Now we have one set of average K_o and α obtained from experimental data and the other set of average K_o and α derived from equation [48] and $K(\theta)$ stemming from the Millington and Quirk method. From these two sets of K_o and α the two theoretical soil-water flux curves from equation [17] are

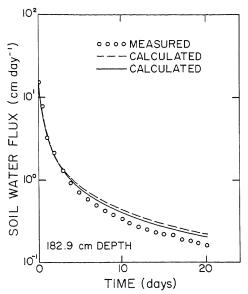


Fig. 25. Average soil-water flux at the 182.9 cm depth as a function of time following the cessation of infiltration. The solid line stems from equation [17] using values of K_o and α stemming from the measured values of $K(\theta)$ given in figure 14. The broken line stems from values of K_o and α estimated by the calculated values of $K(\theta)$ shown in figure 24 at the point (K_o, θ_o) .

given in figure 25 together with the average measured soil-water for the 182.9 cm depth. The solid line is the result of measured values of K_o and α and the broken line stems from estimated values of K_o and α . Allowing for the values of standard deviation shown in table 9, there is good agreement between the two theoretical curves and the experimental data for this depth and others not shown.

CONCLUSIONS AND SUMMARY

The field studied, which was typical of fields in areas of irrigated agriculture, had been graded for efficient production. Although no distinctive well-defined horizon exists throughout the soil profile, it appears from our study that the physical properties at the 120-cm depth are especially important to the over-all hydraulic characteristics

of the soil. For a naturally developed, well-defined soil profile with distinct horizons there will probably be certain horizons which would more or less govern soil-water movement. The physical properties of such a horizon should be extensively studied.

The 150-hectare field studied is fairly uniform in soil classification.

The spatial variation of some of its physical properties (i.e., particle size distribution and bulk density) is well within the permitting limit of a mapping unit (Beckett and Webster, 1971), whereas the steady infiltration rate varied considerably from one plot to another. The steady infiltration rate ranged from 0.5 to 45.7 cm day⁻¹. In terms of the steady hydraulic conductivities, the range was even larger from about 10⁻¹ to (roughly) 10² cm day-1. Recalling that the location and the steady state infiltration value of all 20 experimental plots within the 150-hectare field are given in figure 1, it seems that the field can be roughly subdivided into three units according to the steady infiltration rate. Unit (1) would consist of plots 5, 7, 8, and 20; unit (2) would be plots 1, 3, 4, 6, 9, 10, 11, 12, and 15; unit (3) would be plots 13, 14, 16, 17, and 18. In order to provide more accurate and useful information it may be practical to include the steady state infiltration rate as one of the criterion used in soil classification. Because the steady state infiltration rate was found to be exponentially related to percentage of water saturation, it would be more sensitive than any measure of soilwater content.

We have presented two different ways to evaluate the spatial variability of hydraulic conductivity. First, we presented hydraulic conductivity as a function of percentage of water saturation so that all the hydraulic conductivity versus per cent saturation curves would fall into the limit of per cent saturation between 0 and 100 per cent. The spatial variation of hydraulic conductivity increases with decreased per cent saturation. Secondly, we visualize the field as a homogeneous soil mass and regard soil-water content and hydraulic conductivity as two variables which could be measured separately. At each depth, 20 measurements of soil-water content and hydraulic conductivity were available. Or, at all depths, 120 pairs of values were available for each time period to calculate the mean value and standard deviation of both soil-water content and hydraulic conductivity (fig. 15). Using the information provided by figure 5, equation [17] was successfully applied to predict the soil-water flux at six different depths (fig. 23).

If sufficient information about $K(\theta)$ is not available and only the distributions of K_o and θ_o are known, Millington and Quirk's method (1960) can generate the necessary information about $K(\theta)$ in order to apply equation [17].

It is believed that the statistical approach presented in this text will be applicable to areas larger than the 150-hectare field, provided sufficient information about soil-water characteristics and $K(\theta)$ are available.

As a consequence of this study we conclude:

- 1. Variations in water content are normally distributed with depth and with horizontal distance throughout the field, while values of hydraulic conductivity and soil-water diffusivity are log-normally distributed.
- 2. A simple equation can be used to predict the flux of water leaving any desired depth of soil as a function of time following infiltration. The equation requires only that the steady-state hydraulic conductivity and the slope of the hydraulic conductivity-water content curve near saturation be known.
- 3. Methods available in the literature for predicting hydraulic conductivity versus soil-water content relations from soil-water characteristic curves are adequate for predicting field values.
- 4. Simplified methods for measuring field values of hydraulic conductivity or soil-water diffusivity, using simply a single or preferabley two tensiometers and a reliable soil-water

- characteristic curve, are sufficiently accurate for characterizing conditions.
- 5 Even seemingly uniform land areas manifest large variations in hydraulic conductivity values. Variations in texture, bulk density, and water content are much less. For a given methods for measuring location. water content, hydraulic conductivity, and hydraulic gradients will vield values that are much more accurate than required to characterize an entire field because of the heterogeneity of the soil. Thus, our ability to make predictions over a large area from a single plot can range from good to unsatisfactory, depend-
- ing on the particular prediction parameter of interest.
- 6. The lack of correlation between soilwater parameters and soil-bulk density or particle size implies that measurements made historically during soil surveys have limited value for predicting soil-water movement and retention.
- 7. The most important laboratory measurements for predicting soil-water behavior in the field are the soilwater characteristic curve and a steady-state hydraulic conductivity value. These measurements provide ample information with which to approximately predict the behavior of soil water under field conditions.

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